

ADVANCED General Certificate of Education 2023

Mathematics

Assessment Unit A2 2 assessing Applied Mathematics

AMT21

Centre Number

Candidate Number

[AMT21] TUESDAY 13 JUNE, AFTERNOON

TIME

1 hour 30 minutes.

INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page. You must answer the questions in the spaces provided.

Do not write outside the boxed area on each page or on blank pages.

Complete in black ink only. Questions which require drawing or sketching should be completed using an HB pencil. **Do not write with a gel pen.**

Candidates must answer all questions from sections A and B.

Equal time should be spent on each section. Show clearly the full development of your answers. Answers without working may not gain full credit.

Answers should be given to three significant figures unless otherwise stated.

You are permitted to use a graphic or scientific calculator in this paper.

INFORMATION FOR CANDIDATES

The total mark for this paper is 100. The total available mark for each section of this paper is 50. Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

Answers should include diagrams where appropriate and marks may be awarded for them. Take $g = 9.8 \text{ m s}^{-2}$, unless specified otherwise.

A copy of the Mathematical Formulae and Tables booklet is provided.

Throughout the paper the logarithmic notation used is $\ln z$ where it is noted that $\ln z \equiv \log_e z$ 13316.07 R

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Answer all questions.

SECTION A

Mechanics

1 A	A cannon has a mass of M kg. The cannon which is initially at rest fires a cannonball of mass m kg with a speed				
of $u \mathrm{ms^{-1}}$					
(i)	Find the speed of recoil of the cannon in terms of M , m and u . [5]				
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e	duration of the force acting on the cannon due to the explosion is 0.002 s.
	Find the average force that is exerted on the cannon in terms of m and u . [5]



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2 (In this question, i and j are perpendicular unit vectors in horizontal and vertical directions, respectively.)

A ball is projected from a point whose position vector is 10 **j** m relative to a fixed point O.

The ball's velocity of projection is $(23i + 49j)ms^{-1}$

The ball moves under gravity.

(i) Show that at time *t* seconds after projection, the position vector of the ball relative to O is

[5]

 $[23t \mathbf{i} + (10 + 49t - 4.9t^2) \mathbf{j}] \mathbf{m}$

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3 A uniform thin plank AB has mass M kg and length 6L metres.

C is a point on the plank where AC = 4L metres.

A carpenter places end A on rough horizontal ground and uses a smooth fixed cylinder to support the plank at C as shown in **Fig. 1** below.

The plank rests in equilibrium when inclined at α degrees to the horizontal.



(i) Complete the diagram below showing all the external forces acting on the plank.



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(ii) By taking moments about A find the value of α .	[5
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All	ime t seconds, the particle's displacement x metres from A is given by	
	$r = \frac{1}{2}t^3 + \frac{3}{2}t^2 + 7t (0 \le t \le 2)$	
	$3^{i} + 4^{i} + 7^{i} = (0 - i - 2)^{i}$	
Wh	en $t = 2$ the particle is at B.	
(i)	Find the displacement of B from A.	[2
(ii)	Find its velocity at B.	[4



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For $2 \le t < 4$ the velocity $v \text{ m s}^{-1}$ of the particle can now be modelled as
$v = 14\sec^2\left(\frac{\pi t}{4} - \frac{\pi}{2}\right)$
At $t = 3$ the particle is at C.
(iii) Find the displacement of C from A. [6]
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(iv) If the particle models a train on a straight track, what is the problem with using this model as <i>t</i> gets closer to 4? [2]
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SECTION B

Statistics

5 An economist studies the correlation between unemployment percentage and average income for a large city. He sets up a hypothesis test on ρ , the population correlation coefficient. His hypotheses are:

$$H_0: \rho = 0$$

 $H_1: \rho < 0$

(i) Will the test be one-tailed or two-tailed?

The economist uses a random sample of records over an extended period of time. He calculates the product—moment correlation coefficient for his sample and finds the p-value for the test to be 0.00845

(ii)	Explain what is meant by the term <i>p</i> -value.	[2]
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6	A brewery produces bottles of cider whose volumes are normally distributed with mean μ and variance σ^2
	Given that the upper quartile of the volume of cider in a bottle is 571.71 ml and that 5% of the bottles contain less than 558.95 ml, calculate the values of μ and σ . [10]
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7 It is believed that 1 person in 100 is allergic to milk.

A test has been designed to try to detect the allergy.

For a person with the allergy, there is a 95% chance that the test will give a positive result.

For a person who does not have the allergy, there is a 96% chance that the test will give a negative result.

(i) Using a tree diagram, or otherwise, calculate the probability that a randomly selected person gets a positive result on the test.

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A randomly selected person is tested and the result indicates that they are allergic to milk.

Comment on your answer to (ii).	F11	nd the probability that this person is actually allergic to milk.	[4
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(i)	Calculate the probability that a random call arriving at the switchboard takes between 10 and 15 seconds to be answered.
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The office manager introduces a bonus scheme designed to reduce the amount of time taken for calls to be answered.

He claims that the scheme has been successful.

Following the introduction of the scheme, the office manager calculates the average time taken to answer calls in a random sample of 40 to be 10.8 seconds.

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	t teacher decides to test her suspicion at the 570 level of significance.	The teacher decides to test her suspicion at the 5% level of significance.					
(i)	Explain why a one-tailed test is appropriate in this context.						
		••••••••••					

Daniel took a multiple choice examination in which there were five possible responses

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to each of the questions.

	, write down the num and alternative hypotheses for this test.	۔۔۔۔۔
(iii	i) Describe the meaning of the term level of significance.	[1
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iv) Complete the hypothesis test, stating clearly whether the teacher's suspicion is justified.

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