

Surname	Centre Number	Candidate Number
First name(s)		2



GCE AS/A LEVEL

2305U30-1



S25-2305U30-1

TUESDAY, 20 MAY 2025 – AFTERNOON

FURTHER MATHEMATICS – AS unit 3
FURTHER MECHANICS A

1 hour 30 minutes

ADDITIONAL MATERIALS

In addition to this examination paper, you will need:

- a Formula Booklet;
- a calculator.

INSTRUCTIONS TO CANDIDATES

Use black ink or black ball-point pen. Do not use gel pen or correction fluid.

You may use a pencil for graphs and diagrams only.

Write your name, centre number and candidate number in the spaces at the top of this page.

Answer **all** questions.

Take g as 9.8 ms^{-2} .

Write your answers in the spaces provided in this booklet. If you run out of space, use the additional page(s) at the back of the booklet, taking care to number the question(s) correctly.

INFORMATION FOR CANDIDATES

The maximum mark for this paper is 70.

The number of marks is given in brackets at the end of each question or part-question.

Sufficient working must be shown to demonstrate the **mathematical** method employed.

Answers without working may not gain full credit.

Unless the degree of accuracy is stated in the question, answers should be rounded appropriately.

You are reminded of the necessity for good English and orderly presentation in your answers.

For Examiner's use only		
Question	Maximum Mark	Mark Awarded
1	6	
2	13	
3	11	
4	7	
5	9	
6	10	
7	14	
Total	70	

2305U301
01



JUN252305U30101

1. A particle of mass 1.5 kg is moving under the action of a single force $F \text{ N}$ so that its velocity $v \text{ ms}^{-1}$ at time t seconds is given by

(a) Find an expression for $\mathbf{F}$ at time t s.

[3]



(b) Determine the value of $F.v$ when $t = 2$, clearly stating the units of your answer.

[3]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....



- (b) Given that $m = 5$, calculate the magnitude and direction of the impulse exerted by A on B .

[3]

2305U301
05

(c) Determine the range of values of e to ensure that B will collide with A again. [3]



BLANK PAGE

**PLEASE DO NOT WRITE
ON THIS PAGE**



- (a) Write down the position vectors of A and B at time t seconds.

- $$AB^2 = 53t^2 - 530t + 1650.$$



- (c) Determine the value of t when A and B are closest together. Hence find the least distance between A and B .

[4]



- 
- A diagram showing a car on an inclined plane. The plane is represented by a thick line sloping upwards from left to right. The angle between the plane and the horizontal is labeled α . A car is shown on the incline, facing towards the upper right.

When the car is moving with a constant speed of $v \text{ ms}^{-1}$, it has no tendency to sideslip. The normal reaction of the track on the car is 17 150 N.

- [3]



2305U301
11

[4]



5. A light elastic string, of natural length 1.4 m and modulus of elasticity 156.8 N , has one end attached to a fixed point O and the other end attached to a particle P of mass $m\text{ kg}$.

Initially, P is held at rest at the point O . It is then released and allowed to fall under gravity.

- (a) Determine the extension in the string at the instant when the tension in the string is 36 N .

[2]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

- (b) Given that the kinetic energy of P is 15.12 J when it is 2 m below O , show that $m = 1.8$.

[7]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....





6. A vehicle, of mass 2500 kg, is travelling on a straight road which has a horizontal section followed by an incline. When in motion, the vehicle experiences a variable resistive force of $(1000 + 50v)$ N, where $v \text{ ms}^{-1}$ is the speed of the vehicle.

- (a) Find the power developed by the vehicle's engine when the vehicle is travelling on the horizontal section with a constant speed of 20 ms^{-1} . [4]

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

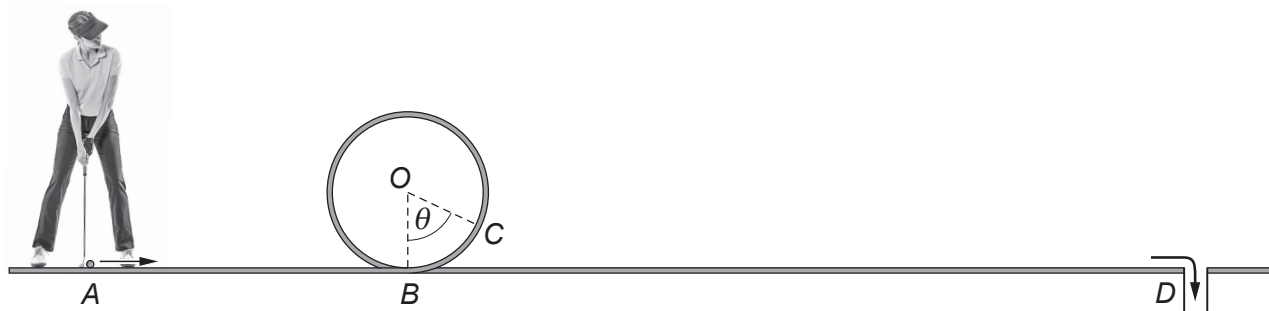


- [illegible]



7. The diagram below shows part of a 'Crazy Golf' course. This part of the course consists of a straight horizontal section AB , leading into a circular loop, followed by another straight horizontal section BD .

The objective of the game is to hit a golf ball, from rest at the point A , so that it remains in contact with the surface for its entire journey until it reaches the point D , where it is required to drop into a hole.



The loop section may be modelled as a vertical circle of radius 0.5 m and the ball as a particle of mass 0.04 kg . You may assume that the entire surface of the course is smooth and is set in the same vertical plane.

The ball is hit horizontally from A . At the point B , which is the lowest point of the circle, the speed of the ball is $u\text{ ms}^{-1}$.

- (a) When the ball is at a point C on the inside of the circular loop, the line OC makes an angle θ with the downward vertical.

- (i) Find, in terms of θ and u^2 , an expression for v^2 , where $v\text{ ms}^{-1}$ is the speed of the ball at C . [4]

- (ii) Show that the reaction of the surface on the ball at C , RN , is given by

$$R = 0.08u^2 - 0.784 + 1.176 \cos \theta. \quad [4]$$

- (iii) Given that the ball does not complete a full circle, but instead, it leaves the loop at a point where $\theta = 120^\circ$, calculate the value of u . [2]

.....

.....

.....

.....





- By using the work-energy principle, determine whether the ball drops into the hole. [4]



[illegible]

[illegible]

[illegible]

[illegible]

BLANK PAGE

**PLEASE DO NOT WRITE
ON THIS PAGE**



BLANK PAGE

**PLEASE DO NOT WRITE
ON THIS PAGE**

