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Other names

**Pearson**  
**Edexcel GCE**

Centre Number

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Candidate Number

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# Mechanics M4

## Advanced/Advanced Subsidiary

Wednesday 15 June 2016 – Morning  
**Time: 1 hour 30 minutes**

Paper Reference

**6680/01**

**You must have:**

Mathematical Formulae and Statistical Tables (Pink)

Total Marks

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**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Whenever a numerical value of  $g$  is required, take  $g = 9.8 \text{ m s}^{-2}$ , and give your answer to either two significant figures or three significant figures.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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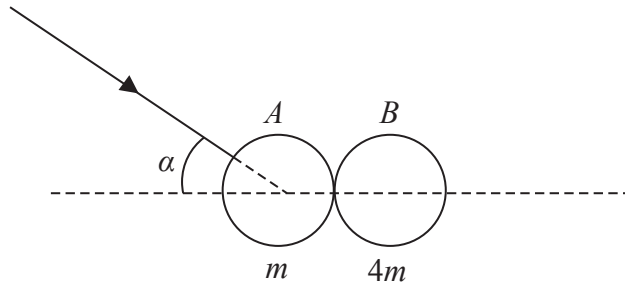
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**PEARSON**

1.



**Figure 1**

A smooth uniform sphere *A* of mass  $m$  is moving on a smooth horizontal plane when it collides with a second smooth uniform sphere *B*, which is at rest on the plane. The sphere *B* has mass  $4m$  and the same radius as *A*. Immediately before the collision the direction of motion of *A* makes an angle  $\alpha$  with the line of centres of the spheres, as shown in Figure 1. The direction of motion of *A* is turned through an angle of  $90^\circ$  by the collision and the coefficient of restitution between the spheres is  $\frac{1}{2}$

Find the value of  $\tan \alpha$ .

**(8)**

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**Question 1 continued**

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Q1

**(Total 8 marks)**



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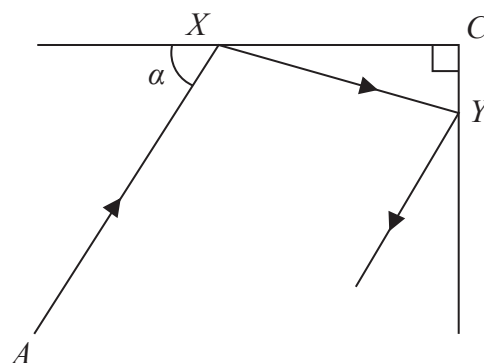


Figure 2

A small spherical ball  $P$  is at rest at the point  $A$  on a smooth horizontal floor. The ball is struck and travels along the floor until it hits a fixed smooth vertical wall at the point  $X$ . The angle between  $AX$  and this wall is  $\alpha$ , where  $\alpha$  is acute. A second fixed smooth vertical wall is perpendicular to the first wall and meets it in a vertical line through the point  $C$  on the floor. The ball rebounds from the first wall and hits the second wall at the point  $Y$ . After  $P$  rebounds from the second wall,  $P$  is travelling in a direction parallel to  $XA$ , as shown in Figure 2. The coefficient of restitution between the ball and the first wall is  $e$ . The coefficient of restitution between the ball and the second wall is  $ke$ .

Find the value of  $k$ .

(9)

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**Question 2 continued**

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**Question 4 continued**

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5. A toy car of mass 0.5 kg is attached to one end  $A$  of a light elastic string  $AB$ , of natural length 1.5 m and modulus of elasticity 27 N. Initially the car is at rest on a smooth horizontal floor and the string lies in a straight line with  $AB = 1.5$  m. The end  $B$  is moved in a straight horizontal line directly away from the car, with constant speed  $u$  m s<sup>-1</sup>. At time  $t$  seconds after  $B$  starts to move, the extension of the string is  $x$  metres and the car has moved a distance  $y$  metres. The effect of air resistance on the car can be ignored.

By modelling the car as a particle, show that, while the string remains taut,

(a) (i)  $x + y = ut$  (2)

(ii)  $\frac{d^2x}{dt^2} + 36x = 0$  (4)

(b) Hence show that the string becomes slack when  $t = \frac{\pi}{6}$  (3)

(c) Find, in terms of  $u$ , the speed of the car when  $t = \frac{\pi}{12}$  (3)

(d) Find, in terms of  $u$ , the distance the car has travelled when it first reaches end  $B$  of the string. (5)

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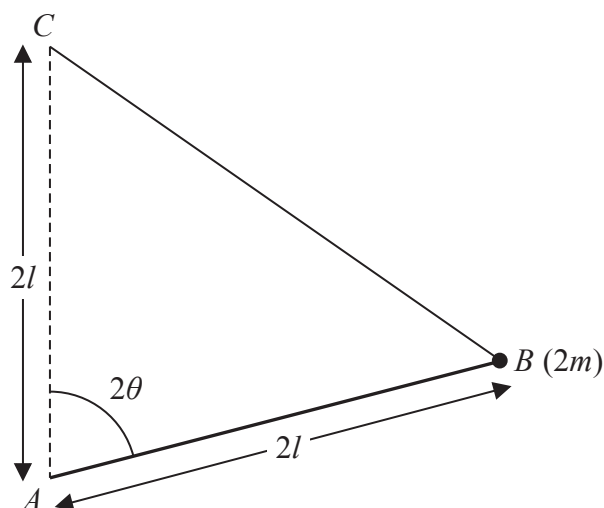


Figure 3

Figure 3 shows a uniform rod  $AB$ , of length  $2l$  and mass  $4m$ . A particle of mass  $2m$  is attached to the rod at  $B$ . The rod can turn freely in a vertical plane about a fixed smooth horizontal axis through  $A$ . One end of a light elastic spring, of natural length  $2l$  and modulus of elasticity  $kmg$ , where  $k > 4$ , is attached to the rod at  $B$ . The other end of the spring is attached to a fixed point  $C$  which is vertically above  $A$ , where  $AC = 2l$ . The angle  $BAC$  is  $2\theta$ , where  $\frac{\pi}{6} < \theta \leq \frac{\pi}{2}$

(a) Show that the potential energy of the system is

$$4mgl\{(k - 4)\sin^2 \theta - k \sin \theta\} + \text{constant} \tag{6}$$

Given that there is a position of equilibrium with  $\theta \neq \frac{\pi}{2}$

(b) show that  $k > 8$  (6)

Given that  $k = 10$

(c) determine the stability of this position of equilibrium. (4)

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