



Rewarding Learning

**General Certificate of Secondary Education
2016**

Mathematics

Unit T4

(With calculator)

Higher Tier

[GMT41]

THURSDAY 26 MAY, 9.15 am–11.15 am

**MARK
SCHEME**

GCSE MATHEMATICS

Introduction

The mark scheme normally provides the most popular solution to each question. Other solutions given by candidates are evaluated and credit given as appropriate; these alternative methods are not usually illustrated in the published mark scheme.

The solution to a question gains marks for correct method and marks for accurate working based on this method. The marks awarded for each question are shown in the right hand column and they are prefixed by the letters **M**, **A** and **MA** as appropriate. The key to the mark scheme is given below:

M indicates marks for correct method.

A indicates marks for accurate working, whether in calculation, reading from tables, graphs or answers. Accuracy marks may depend on preceding **M** (method) marks, hence **M0 A1** cannot be awarded, i.e. where the method is not correct no marks can be given.

MA indicates marks for combined method and accurate working.

C indicates marks for quality of written communication.

A later part of a question may require a candidate to use an answer obtained from an earlier part of the same question. A candidate who gets the wrong answer to the earlier part and goes on to the later part is naturally unaware that the wrong data is being used and is actually undertaking the solution of a parallel problem from the point at which the error occurred. If such a candidate continues to apply correct method, then the candidate's individual working must be **followed through** from the error. If no further errors are made, then the candidate is penalised only for the initial error. Solutions containing two or more working or transcription errors are treated in the same way. This process is usually referred to as "follow-through marking" and allows a candidate to gain credit for that part of a solution which follows a working or transcription error.

It should be noted that where an error trivialises a question, or changes the nature of the skills being tested, then as a general rule, it would be the case that not more than half the marks for that question or part of that question would be awarded; in some cases the error may be such that no marks would be awarded.

Positive marking:

It is our intention to reward candidates for any demonstration of relevant knowledge, skills or understanding. For this reason we adopt a policy of **following through** their answers, that is, having penalised a candidate for an error, we mark the succeeding parts of the question using the candidate's value or answers and award marks accordingly.

Some common examples of this occur in the following cases:

- (a) a numerical error in one entry in a table of values might lead to several answers being incorrect, but these might not be essentially separate errors;
- (b) readings taken from candidates' inaccurate graphs may not agree with the answers expected but might be consistent with the graphs drawn.

When the candidate misreads a question in such a way as to make the question easier, only a proportion of the marks will be available (based on the professional judgement of the examiner).

General Marking Advice

- (i) If the correct answer is seen in the body of the script and the answer given in the answer line is clearly a transcription error, full marks should be awarded.
- (ii) If the answer is missing, but the correct answer is seen in the body of the script, full marks should be awarded.
- (iii) If the correct answer is seen in working but a completely different answer is seen in the answer space, then some marks will be awarded depending on the severity of the error.
- (iv) Work crossed out but not replaced should be marked.
- (v) In general, if two or more methods are offered, mark only the method that leads to the answer on the answer line. If two (or more) answers are offered (with no solution offered on the answer line), mark the poorest answer.
- (vi) For methods not provided for in the mark scheme, give as far as possible equivalent marks for equivalent work.
- (vii) Where a follow through mark is indicated on the mark scheme for a particular part question, the marker must ensure that you refer back to the answer of the previous part of the question.
- (viii) Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures seen. E.g. the answer in the mark scheme is 4.65 and the candidate then correctly rounds to 4.7 or 5 on the answer line. Allow full marks for 4.65 seen in the working.
- (ix) Anything in the mark scheme which is in brackets (...) is not required for the mark to be earned, but if present it must be correct.
- (x) For any question, the range of answers given in the mark scheme is inclusive.

Quality of written communication

In GCSE Mathematics, particular questions are identified where candidates must demonstrate the quality of their written communication.

In particular, candidates must:

- (i) ensure that text is legible and that spelling, punctuation and grammar are accurate so that meaning is clear (i.e. comprehension and meaning is clear by using the correct notation and labelling conventions);
- (ii) select and use a form and style of writing appropriate to their purpose and to complex subject matter (i.e. reasoning, explanation or argument is correct and appropriately structured to convey mathematical reasoning); and
- (iii) organise information clearly and coherently, using specialist vocabulary where appropriate (i.e. the mathematical methods and processes used are coherently and clearly organised and appropriate mathematical vocabulary used).

This assessment may be through, for example, an explanation of the geometrical properties of a given shape or, for example, through concise mathematical argument in a multi-step problem.

		AVAILABLE MARKS	
1	(a) 4, 10, 26, 50, 80, 96, 108, 112	A1	
	(b) Cumulative frequency graph	M1 A1	
	(c) (i) From their graph	A1	
	(ii) Readings at 28 and 84	A1	
	Correct subtraction	A1	
	(d) 112 – their reading	MA1	
	Expressed as % of 112	MA1	8
2	sin identified	MA1	
	$\sin A = \frac{4}{6.5}$	MA1	
	$A = 38^\circ$	A1	
	tan identified	MA1	
	$\tan 52 = \frac{4}{DC}$ or $\tan 38 = \frac{DC}{4}$	A1	
	$DC = 3.12\text{ m}$	A1	6
3	$\frac{315}{360} \times \pi \times 8^2$	MA2	
	$= 175.9\text{ cm}^2$	A1	3
4	900 ml = 120%	MA1	
	$\frac{900}{120} \times 100 = 750$	MA1 A1	3
5	Maximum weight of coffee and jar = 672.5 g	MA1	
	Minimum weight of jar = 447.5 g	MA1	
	Maximum weight of coffee = 672.5 – 447.5		
	= 225 g	MA1	3
6	$6x - 2y = 14$	MA1	
	$15x - 5y = 35$		
	$\frac{5x - 2y = 10}{x = 4}$ or $\frac{15x - 6y = 30}{y = 5}$	MA1	
	$y = 5$	MA1	3
	$x = 4$		

			AVAILABLE MARKS
7	(a) $6x^2 + 8x - 9x - 12$ $= 6x^2 - x - 12$	MA1 MA1	5
	(b) $(p - 8)(p + 8)$	A1	
	(c) $\frac{x}{3h^2}$	A2	
8	(a) Gradient = 3	A1	6
	(b) $y = 3x + 1$	A1	
	(c) $y = 3x - 1$	A1 A1	
	(d) Gradients are 3 and $-\frac{1}{3}$. Gradients multiply to give -1	A1 A1	
9	Multiples of 15 and 9 given 45 minutes identified as the 'lowest common multiple' 5 laps for Jenna and 3 for Luke gives a difference of 2 laps	MA1 A1 A1	3
10	(a) Range will not be affected because highest and lowest values in first and last groups have not been amended	C1 C1	5
	(b) Mean will be lowered As the two new values are in lower regions of data and will lower the overall mean	C1 C1	
	(c) $20 \leq x < 40$	A1	
11	$2L = 3B$	MA1	5
	$L + B = 20$	MA1	
	$\frac{3B}{2} + B = 20$		
	so $B = \frac{20}{2.5} = 8$	MA1	
	$L = 12$	MA1	
	Area = $20 \times 24 = 480$	MA1	
12	(a) f.d. 2 12 8 2 0.25 Scales and labels Bars	MA1 A1 A1	5
	(b) Using 80, 34	MA1	
	Sample required = $\frac{34}{80} \times 20 = 8$ or 9	MA1	

			AVAILABLE MARKS
13	$x(x + 3) = (x - 2)(x + 6)$	MA1	4
	$x^2 + 3x = x^2 + 4x - 12$	MA1	
	$x = 12$	A1	
	New length = 18 New width = 10	A1	
14 (a)	$960 = k \times 64$	MA1	4
	$k = 15$ hence $Y = 15X^3$	MA1	
	(b) $\frac{405}{15} = X^3$	MA1	
		$X = 3$	
15 (a)	$2^{\frac{2}{3}n} = 2^4$	MA1	5
	$\frac{2}{3}n = 4 \quad n = 6$	A1	
	(b) $(9 + 16)^{-m} = \frac{1}{5}$	A1	
		$5^{-2m} = 5^{-1}$	
$m = \frac{1}{2}$	A1		
16 (a)	$\sqrt{(36^2 + 20^2 + 25^2)}$	M1	5
	$= 48.17675\dots$	A1	
Alternative method			
	$\sqrt{(36^2 + 20^2)} = 41.18252056$	MA1	5
	$\sqrt{(41.18252056^2 + 25^2)} = 48.17675\dots$	MA1	
(b)	Diagonal of base = 41.18252056	MA1	A1 5
	$\text{Tan } \alpha = \frac{25}{41.18252056}$	MA1	
	$\alpha = 31.3^\circ$		
17 (a)	0–20 20		7
	20–50 90		
	50–80 75		
	80–100 36		
	100–120 4	MA2	
	$\frac{20 \times 10 + 90 \times 35 + 75 \times 65 + 36 \times 90 + 4 \times 110}{225}$	MA1	
	$= \frac{11905}{225} = 52.9$	A1	
(b)	75 less M (or 150 more than M) so 55 in second group (so 35 in second group)	MA1	
	$\frac{55}{90}$ of 30 is 18.3	A1	
	M = 38.3 minutes	A1	

		AVAILABLE MARKS	
18	OST and OQT = 90 (angles between tangent and radius)	C1	
	SOQ = 360 - 90 - 90 - x = 180 - x (sum of quad)	C1	
	SOQ reflex = 360 - (180 - x) = 180 + x	C1	
	SPQ = $\frac{1}{2}(180 + x) = 90 + \frac{x}{2}$ (angle at circumference = half angle at centre)	C1	
QWC fully explained at each stage		C1	
Alternative method			
18	OST and OQT = 90 (angles between tangent and radius)	C1	
	SOQ = 360 - 90 - 90 - x = 180 - x (sum of quad)	C1	
	QRS = 90 - $\frac{x}{2}$ (angle at circumference = half angle at centre)	C1	
	SPQ = 180 - (90 - $\frac{x}{2}$) = 90 + $\frac{x}{2}$ (opposite angles in CQ = 180)	C1	
	QWC fully explained at each stage	C1	
19	$\frac{2(3a - 4)(a + 2)}{2(2 - a)(2 + a)}$	MA1	
	$\frac{(3a - 4)}{(2 - a)}$	MA1	
20	$\frac{(3a - 4)}{(2 - a)}$	A1	
	20	$2x^2 + 3(x + 1)^2 = 2$	MA2
	$2x^2 + 3(x^2 + 2x + 1) = 2$	MA1	
	$5x^2 + 6x + 1 = 0$	MA1	
	$(5x + 1)(x + 1) = 0$	MA1	
$x = -\frac{1}{5}$ and $x = -1$	MA1		
$y = \frac{4}{5}$ and $y = 0$	MA1		
20	or	$2(y - 1)^2 + 3y^2 = 2$	MA2
	$2(y^2 - 2y + 1) + 3y^2 = 2$	MA1	
	$5y^2 - 4y = 0$	MA1	
	$y(5y - 4) = 0$	MA1	
	$y = 0$ and $y = \frac{4}{5}$	MA1	
$x = -1$ and $y = -\frac{1}{5}$	MA1		
21	$y + z = 3(y - z)$	MA1	
	$y + z = 3y - 3z$	MA1	
	$4z = 2y$		
	$2z = y$	MA1	
Hence $\frac{2z + 3z}{2z - 3z} = \frac{5z}{-z} = -5$		MA1 A1	
Total		100	