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Summer 2018
Publications Code 6691_01_1806_MS
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General Marking Guidance

• All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.

• Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.

• Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.

• There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.

• All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate’s response is not worthy of credit according to the mark scheme.

• Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.

• Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.
EDEXCEL GCE MATHEMATICS

General Instructions for Marking

1. The total number of marks for the paper is 75.

2. The Edexcel Mathematics mark schemes use the following types of marks:
   - **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
   - **A** marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
   - **B** marks are unconditional accuracy marks (independent of M marks)
   - Marks should not be subdivided.

3. Abbreviations

   These are some of the traditional marking abbreviations that will appear in the mark schemes.
   - bod – benefit of doubt
   - ft – follow through
   - the symbol \(\checkmark\) will be used for correct ft
   - cao – correct answer only
   - cso - correct solution only. There must be no errors in this part of the question to obtain this mark
   - isw – ignore subsequent working
   - awrt – answers which round to
   - SC: special case
   - oe – or equivalent (and appropriate)
   - dep – dependent
   - indep – independent
   - dp decimal places
   - sf significant figures
   - \* The answer is printed on the paper
   - The second mark is dependent on gaining the first mark

4. All A marks are ‘correct answer only’ (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.

6. If a candidate makes more than one attempt at any question:
   - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
   - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer
Question Number | Scheme | Marks
---|---|---
1. (a) | \[ r = \frac{S_y}{\sqrt{S_y S_x}} = \frac{47.7625}{\sqrt{34787.5 \times 0.217287}} = 0.549361... \] | B1

(b) \[ H_0 : \rho = 0, H_1 : \rho > 0 \]
\[ (0.549 < 0.6215 \text{ (Not significant Insufficient evidence to reject } H_0) \]
Insufficient evidence of a positive correlation between the concentration of a radioactive element and the amount of dissolved solids in groundwater.

<table>
<thead>
<tr>
<th>Sample</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>G</th>
<th>H</th>
</tr>
</thead>
<tbody>
<tr>
<td>c</td>
<td>2</td>
<td>6</td>
<td>4</td>
<td>3</td>
<td>7</td>
<td>1</td>
<td>8</td>
<td>5</td>
</tr>
<tr>
<td>a</td>
<td>4</td>
<td>5</td>
<td>1</td>
<td>3</td>
<td>8</td>
<td>2</td>
<td>6</td>
<td>7</td>
</tr>
<tr>
<td>d</td>
<td>-2</td>
<td>1</td>
<td>3</td>
<td>0</td>
<td>-1</td>
<td>-1</td>
<td>2</td>
<td>-2</td>
</tr>
<tr>
<td>( d^2 )</td>
<td>4</td>
<td>1</td>
<td>9</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>4</td>
<td>4</td>
</tr>
</tbody>
</table>

Note Reverse ranks \( \sum d^2 = 144 \)
\[ r = 1 - \frac{6 \sum d^2}{n(n^2 - 1)} = 1 - \frac{6 \times 24}{8(64 - 1)} = 0.71428... \] | M1A1

(d) \[ H_0 : \rho_s = 0, H_1 : \rho_s > 0 \]
\[ (0.714 > 0.6429 \text{ (Significant. Reject } H_0) \]
Evidence of a positive correlation between the concentration of a radioactive element and the amount of dissolved solids in groundwater.

(e) Results of tests suggest (monotonic) non-linear relationship or assumptions for PMCC breached i.e. not (joint) normal.

**Notes**

(a) 1st B1 awrt 0.549
(b) 1st B1 Both correct. Require population parameter \( \rho \) and one tailed test.
2nd B1 cv 0.6215
3rd B1 Context required. Must mention concentration of a radioactive element and amount of dissolved solids
(c) 1st M1 for an attempt to rank the concentration of a radioactive element and the amount of dissolved solids with at least 4 correct for each variable. Allow reverse ranks.
2nd M1 for attempt at \( d^2 \) row
1st A1 all correct
3rd M1 for use of the correct formula and an attempt to rank, follow through their \( \sum d^2 \) if clearly stated
If answer is not correct, a correct expression is required.
A1 awrt 0.714
(d) 1st B1 for both hypotheses in terms of \( \rho \), one tail \( H_1 \). Allow use of \( \rho_s \).
Alternative hypothesis compatible with their ranking.
2nd B1 for cv of 0.6429
3rd B1ft for a correct contextualised comment. Must mention concentration of a radioactive element and the amount of dissolved solids. Follow through their \( r_s \) and their cv (provided it is \( |cv| < 1 \))
Don’t insist on the word “positive” for a one-tailed test.
B1 for ‘non-linear’ oe, or ‘not normal’
<table>
<thead>
<tr>
<th>Question Number</th>
<th>Scheme</th>
<th>Marks</th>
</tr>
</thead>
</table>
| 2. (a) | **Record / List** all ticket numbers of **standard** and **premium** tickets  
**Use random numbers** to select a sample of standard and a sample of premium ticket holders  
**i.e. within strata.**  
**Sample sizes in proportion** to the no of standard and no of premium ticket holders at the concert. | B1 | (3) |
| (b) | \[H_0 : \mu_p - \mu_s = 6 \quad \text{oe} \quad [ \ p = \text{premium} \ s = \text{standard} ]\]  
\[H_1 : \mu_p - \mu_s > 6 \quad \text{oe}\]  
Standard error:  
\[z = \frac{\pm (23 - 15 - 6)}{\sqrt{\frac{10^2}{60} + \frac{8^2}{55}}} = \left[\sqrt{2.83030...}\right] = [1.682...]\]  
\[= \pm 1.1888... \quad \text{awrt} \pm 1.19\]  
\[\text{cv 5% one tailed} = 1.6449\]  
Not significant, insufficient evidence to reject \(H_0\)  
Insufficient evidence to support the **manager’s claim**  
or the mean value of merchandise sold to premium ticket holders is NOT more than £6 greater than the mean value of merchandise sold to standard ticket holders. | B1 | B1 |
| (c) | **Sample size is large so Central Limit Theorem (CLT) applies** so  
do not need to assume **merchandise sold** has a normal distribution. | B1 |

**Notes**

(a)  
1st B1 **Sampling frame in context. Accept list of all standard and premium ticket holders at the concert.**  
2nd B1 **Use of random selection eg simple random sampling within strata**  
3rd B1 **Accept description of \(n_s, n_p\).**  
(b)  
1st & 2nd B1 for hypotheses. **Accept \(\mu_s, \mu_p\) or \(\mu_s, \mu_p\) etc if it is clear which is which.**  
1st M1 for an attempt at se with 3 out of 4 values correct.  
2nd dM1 dependent on 1st M1 for a correct numerator (must have - 6) and fit their se.  
1st A1 for awrt 1.19  
3rd B1 for \(\pm 1.6449\) seen or probability of awrt 0.117, Sign must match their test statistic.  
3rd dM1 dep. on 1st M1 for a correct statement based on their normal cv and their test statistic. Ignore their hypotheses. Allow accept \(H_0\) but reject \(H_1\) is M0. Can be implied by correct conclusion.  
2nd A1cso for correct comment in context dependent upon all other marks being awarded.  
**Must** mention merchandise, standard and premium ticket holders and \(6\) or manager and belief or claim  
NB **Use of cv for difference in means \(D\) will have \(D = 6 + 1.6449 \times \text{s.e.} = \text{awrt} 8.33\) and requires sight of \(d = 8\) with a comment for the 3rd M1  
(c)  
1st B1 for mentioning large samples and **CLT**  
2nd dB1 dependent on 1st B1 for stating **no need to** assume normality. Require merchandise sold not mean merchandise sold.
<table>
<thead>
<tr>
<th>Question Number</th>
<th>Scheme</th>
<th>Marks</th>
</tr>
</thead>
<tbody>
<tr>
<td>3. (a)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\bar{x} = \hat{\mu} = 1.55$</td>
<td>cao 1.55</td>
<td>B1</td>
</tr>
<tr>
<td>$s^2 = \frac{n \sum x^2 - 4 \times 1.55^2}{n} = 17$</td>
<td>awrt 0.057</td>
<td>M1A1ftA1</td>
</tr>
<tr>
<td>$\sum x^2 = 9.78, &quot;\sum x^2&quot; &gt; 9.61, &quot;\sum x^2&quot; \neq (\sum x)^2 = 38.44$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Or $s^2 = \frac{0.25^2 + 0.15^2 + 0.15^2 + 0.25^2}{3} = 17$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>(b) $P({\mu - \hat{\mu}} &lt; 0.1) = 0.99$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$0.1 \div 0.5 = 2.5758$</td>
<td></td>
<td>M1B1A1ft</td>
</tr>
<tr>
<td>$\sqrt{n}$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$n = \left(\frac{2.5758 \times 0.5}{0.1}\right)^2 = 12.879^2 = 165.8...$</td>
<td></td>
<td>dM1A1ft</td>
</tr>
<tr>
<td>Sample size $(n \geq 166)$</td>
<td></td>
<td>A1 cao</td>
</tr>
</tbody>
</table>

**Notes**

(a) 1st B1 1.55 correct answer only
1st M1 for a correct expression ft their $\bar{x}$
1st A1 for a fully correct expression ft their $\bar{x}$ only
2nd A1 accept awrt 0.057

(b) 1st M1 $\frac{0.1}{\text{their } x} = z$ value. Accept with an inequality in any direction.
$\sqrt{n}$
1st B1 2.5758
1st A1 for any equivalent form. Allow $ft$ of $z = 2.326$ or awrt 3.090. Must use 0.5
2nd dM1 for attempt to solve for $n$ dependent on 1st M leading to $n = $
2nd A1 for $\left(\frac{2.5758 \times 0.5}{0.1}\right)^2$ Allow $ft$ for 135.2... or 238.7...
3rd A1 for 166 cao
<table>
<thead>
<tr>
<th>Question Number</th>
<th>Scheme</th>
<th>Marks</th>
</tr>
</thead>
<tbody>
<tr>
<td>4. (a)</td>
<td>(2 \times 2.5758 \times \frac{\sigma}{\sqrt{120}} = 0.47027...\sigma)</td>
<td>M1B1A1 (3)</td>
</tr>
</tbody>
</table>
| (b)             | \(H_0 : \mu = 6 \quad H_1 : \mu \neq 6\)  
(Significance level = 10\%)  
(6 is in the interval so not significant, do not reject \(H_0\) \(\mu = 6\)) | B1 B1 B1 (3) |
| (c)             | \(1.6449 \times \frac{\sigma}{\sqrt{100}} = (6.25 - 5.14) / 2(= 0.555)\)  
\(\sigma = 3.374...\) | M1B1 A1 (3) |

### Notes

(a) 1st M1 Use of \(2 \frac{z}{\sqrt{n}}\) with \(z > 2\)
1st B1 2.58 or better
1st A1 awrt 0.47 \(\sigma\)

(b) 1st B1 Both hypotheses in terms of \(\mu\).
2nd B1 10\%
3rd B1 Correct comment leading to accepting \(H_0\)

(c) 1st M1 for \(z \frac{\sigma}{\sqrt{100}} = 0.555\) oe, using \(n = 100\) and where \(|z| > 1.5\)
1st B1 for 1.6449 or better in an attempt (could be 1.6449 \(\sigma = c\) or even 1.6449 \(\sigma^2 = c\))
1st A1 awrt 3.37. Allow awrt 3.38 from use of \(z = 1.64\)
<table>
<thead>
<tr>
<th>Question Number</th>
<th>Scheme</th>
<th>Marks</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 (a)</td>
<td>(Let $W = L - 3C$)</td>
<td>B1, B1</td>
</tr>
<tr>
<td></td>
<td>$E(W) = 2800 - 3 \times 1000 = -200$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$Var(W) = 650^2 + 3^2 \times 250^2 = 985000$</td>
<td>M1A1</td>
</tr>
<tr>
<td></td>
<td>$P(W &gt; 0) = P(Z &gt; \frac{200}{\sqrt{985000}}) = P(Z &gt; 0.20157...), = 0.42015$ (calc) or $0.4207$ (tables)</td>
<td>dM1, A1</td>
</tr>
<tr>
<td>5 (b)</td>
<td>($F = C_1 + C_2 + \ldots + C_s + L_1 + L_2 + L_s$)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$E(F) = 16400$</td>
<td>B1</td>
</tr>
<tr>
<td></td>
<td>$Var(F) = 8 \times 250^2 + 3 \times 650^2 = 1767500$</td>
<td>M1A1</td>
</tr>
<tr>
<td></td>
<td>$P(F &gt; 20000) = P(Z &gt; \frac{20000 - 16400}{\sqrt{1767500}}) = P(Z &gt; 2.7078...), = 0.003386$ (calc) or $0.0035$ (interpolation)</td>
<td>dM1, A1</td>
</tr>
<tr>
<td>5 (c)</td>
<td>Assume <strong>selection</strong> of cars and lorries is <strong>random</strong>. <strong>Weights</strong> of cars and lorries are <strong>independent</strong>.</td>
<td>B1</td>
</tr>
</tbody>
</table>

**Notes**

(a) 1<sup>st</sup> B1 for forming a suitable variable. May be implied by correct variance.

2<sup>nd</sup> B1 for $-200$ cao or $200$ if their $W = 3C - L$

1<sup>st</sup> M1 for attempting $Var(W) = Var(L) + 3^2 \times Var(C)$. Condone swapping $L$ and $C$.

1<sup>st</sup> A1 for $985000$ cao

2<sup>nd</sup> M1 dependent upon first M1 for standardising with their $-200$ and their $985000$

2<sup>nd</sup> A1 awrt $0.420-0.421$

(b) 1<sup>st</sup> B1 for $164000$ cao

1<sup>st</sup> M1 for attempting $Var(F) = 8 \times Var(C) + 3 \times Var(L)$

1<sup>st</sup> A1 for $1767500$ cao

2<sup>nd</sup> M1 dependent upon first M1 for standardising with their $164000$ and their $1767500$

2<sup>nd</sup> A1 awrt $0.003-0.004$

(c) Either random selection or independent weights

Total 12
(a) $H_0: B(4, 0.5)$ is a suitable model $H_1: B(4, 0.5)$ is not a suitable model

<table>
<thead>
<tr>
<th>Even number count</th>
<th>$O_i$</th>
<th>$E_i$</th>
<th>$(O_i - E_i)^2 / E_i$</th>
<th>$O_i^2 / E_i$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>12</td>
<td>9.375</td>
<td>0.735</td>
<td>15.36</td>
</tr>
<tr>
<td>1</td>
<td>45</td>
<td>37.5</td>
<td>1.5</td>
<td>54</td>
</tr>
<tr>
<td>2</td>
<td>36</td>
<td>56.25</td>
<td>7.29</td>
<td>23.04</td>
</tr>
<tr>
<td>3</td>
<td>39</td>
<td>37.5</td>
<td>0.06</td>
<td>40.56</td>
</tr>
<tr>
<td>4</td>
<td>18</td>
<td>9.375</td>
<td>7.935</td>
<td>34.56</td>
</tr>
</tbody>
</table>

$E_i = 150 \times P(X = i)$

$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$ or $\chi^2 = 2 \sum \frac{O_i^2}{E_i} - N$

$\chi^2 = 17.52$ or $\chi = 167.52 - 150 = 17.52$ awrt 17.5

$\nu = 4$, $\chi^2(1\%) = 13.277$

(Reject $H_0$,) $B(4,0.5)$ is not a suitable model or David’s claim incorrect.

(b) $\hat{p} = \frac{0 \times 12 + 1 \times 45 + 2 \times 36 + 3 \times 39 + 4 \times 18}{4 \times 150} = 0.51$

(c) $d = 150 \times 6 \times 0.51^2 \times 0.49^2 = 56.205009$ awrt 56.2

$e = 150 - (8.65 + 36.00 + 39.00 + "d") = 10.144991$ awrt 10.1 or 10.2

or $e = 150 \times 0.51^4 = 10.1478015$

(d) $H_0: B(4, p)$ is a suitable model $H_1: B(4, p)$ is not a suitable model

(e) $\nu = 3$, $\chi^2(1\%) = 11.345$

(16.9>11.345) Reject $H_0$

Binomial is not a suitable model or John’s claim incorrect or equivalent contextualised statement that rejects the Binomial model.

Notes

(a) 1st B1 Accept ‘Binomial with $p = 0.5$’ replacing ‘B(4, 0.5)’

1st M1 for attempt at $E_i = 150 \times P(X = i)$ with at least 2 values correct.

1st A1 at least 4 $E_i$ correct to 3sf cao. Condone truncation.

2nd M1 for at least 2 correct calculations from 4th or 5th column.

2nd A1 at least 4 correct to 3sf from 4th or 5th column. Condone truncation.

3rd A1 for a test statistic of awrt 17.5 Answer only implies 2ndM1 2ndA1 3rdA1

4th A1 for correct conclusion rejecting binomial model. Condone missing parameters here. Award provided their test statistic >11.345

(b) 1st B1 for attempting $\hat{p} = \frac{\sum_{600}}{6}$ with at least 2 values on the numerator correct

1st A1 for 0.51 cao

(c) 1st M1 $d = 150 \times 6 \times (their \hat{p})^2 \times (1 - their \hat{p})^2$

1st A1 awrt 56.2

1st B1ft awrt 10.1 or follow from "d"

(d) 1st B1 accept $H_0$: Binomial is a suitable model $H_1$: Binomial is not a suitable model

(e) 1st B1 $\nu = 3$, 2nd B1 11.345, follow through their $\nu$ ≠ their value in part (a)

3rd B1 Correct statement rejecting $H_0$