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National  
Qualifications  
2022 MODIFIED

Mark

**X847/75/01**

# Mathematics Paper 1 (Non-calculator)

WEDNESDAY, 4 MAY

9:00 AM – 10:00 AM



\* X 8 4 7 7 5 0 1 \*

Fill in these boxes and read what is printed below.

Full name of centre

Town

Forename(s)

Surname

Number of seat

Date of birth

Day

Month

Year

Scottish candidate number

**Total marks — 40**

Attempt ALL questions.

**You may NOT use a calculator.**

To earn full marks you must show your working in your answers.

State the units for your answer where appropriate.

Write your answers clearly in the spaces provided in this booklet. Additional space for answers is provided at the end of this booklet. If you use this space you must clearly identify the question number you are attempting.

Use **blue** or **black** ink.

Before leaving the examination room you must give this booklet to the Invigilator; if you do not, you may lose all the marks for this paper.



\* X 8 4 7 7 5 0 1 0 1 \*

## FORMULAE LIST

The roots of  $ax^2 + bx + c = 0$  are  $x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$

Sine rule  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule  $a^2 = b^2 + c^2 - 2bc \cos A$  or  $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$

Area of a triangle  $A = \frac{1}{2}ab \sin C$

Volume of a sphere  $V = \frac{4}{3}\pi r^3$

Volume of a cone  $V = \frac{1}{3}\pi r^2 h$

Volume of a pyramid  $V = \frac{1}{3}Ah$

Standard deviation  $s = \sqrt{\frac{\Sigma(x - \bar{x})^2}{n - 1}}$

or  $s = \sqrt{\frac{\Sigma x^2 - \frac{(\Sigma x)^2}{n}}{n - 1}}$ , where  $n$  is the sample size.



\* X 8 4 7 7 5 0 1 0 2 \*

Total marks — 40  
 Attempt ALL questions

1. Evaluate

$$\frac{2}{3} \left( \frac{1}{5} + \frac{3}{4} \right).$$

Give your answer in its simplest form.

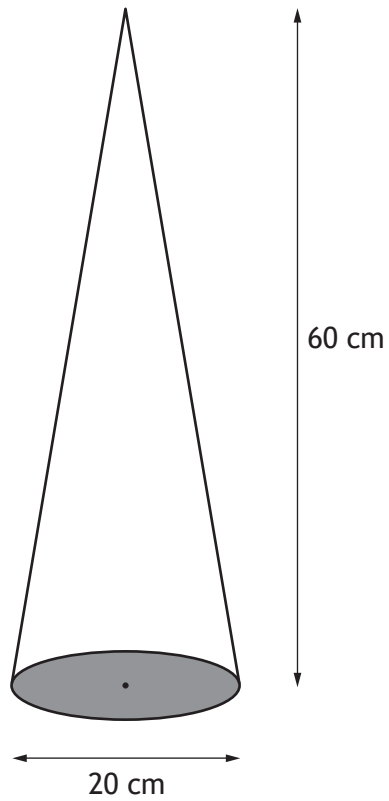
2

2. Given that  $f(x) = x^3 - 2$ , evaluate  $f(-3)$ .

2



3. The diagram below shows a cone with diameter 20 centimetres and height 60 centimetres.



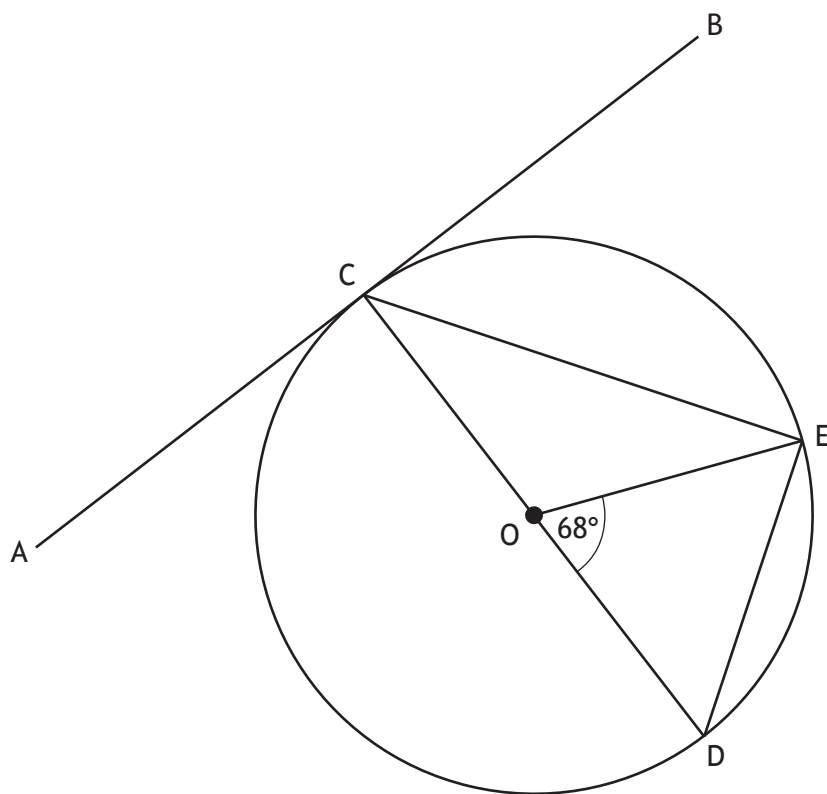
Calculate the volume of the cone.

Take  $\pi = 3.14$ .

2



4. The diagram below shows a circle with centre O.



AB is a tangent to the circle at the point C.

CD is a diameter of the circle.

Angle EOD is  $68^\circ$ .

Calculate the size of angle ACE.

3

Angle ACE =



5. (a) Express  $x^2 + 8x + 15$  in the form  $(x + a)^2 + b$ .

2

(b) Hence, or otherwise, state the coordinates of the turning point of the graph of  $f(x) = x^2 + 8x + 15$ .

1

6. Find the equation of the line passing through the points  $(-3, -1)$  and  $(-5, 7)$ .  
Give the equation in its simplest form.

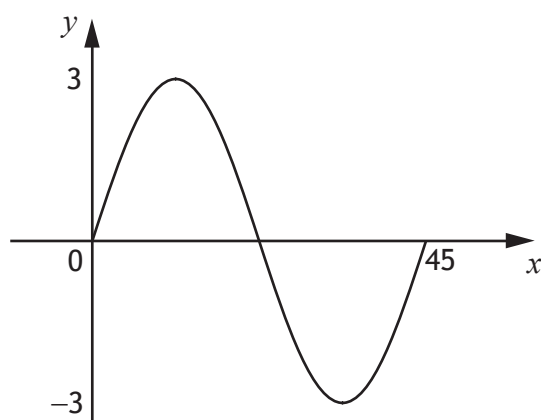
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7. Change the subject of the formula  $D = \frac{B+4}{C^2}$  to  $B$ .

2

8. Part of the graph of  $y = a \sin bx^\circ$  is shown in the diagram.



(a) State the value of  $a$ .

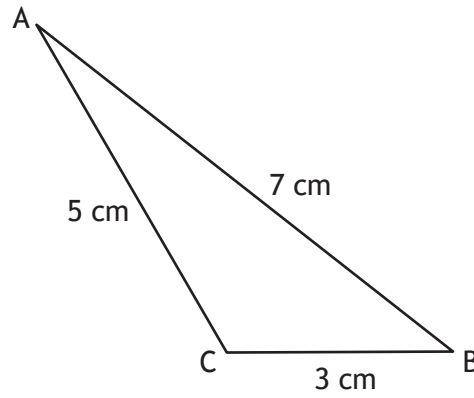
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(b) State the value of  $b$ .

1



9. The diagram shows triangle ABC.



- $AB = 7$  centimetres
- $BC = 3$  centimetres
- $AC = 5$  centimetres

Calculate the value of  $\cos B$ .

Give your answer in its simplest form.

2





10. Tommy buys flower seeds from a website.  
Tommy is given a 30% discount. He pays £16.10 for the seeds.  
Calculate the cost of the flower seeds without the discount.

3

11. Simplify  $(m^{-2})^4 \times m^{-5}$ .  
Give your answer with a **positive** power.

3



\* X 8 4 7 7 5 0 1 0 9 \*

12. Express  $\frac{4}{x+2} \div \frac{5}{(x+2)^2}$ ,  $x \neq -2$  as a single fraction in its simplest form.

2

13. Expand and simplify  $\sqrt{10}(\sqrt{10} - \sqrt{2}) + 8\sqrt{5}$ .

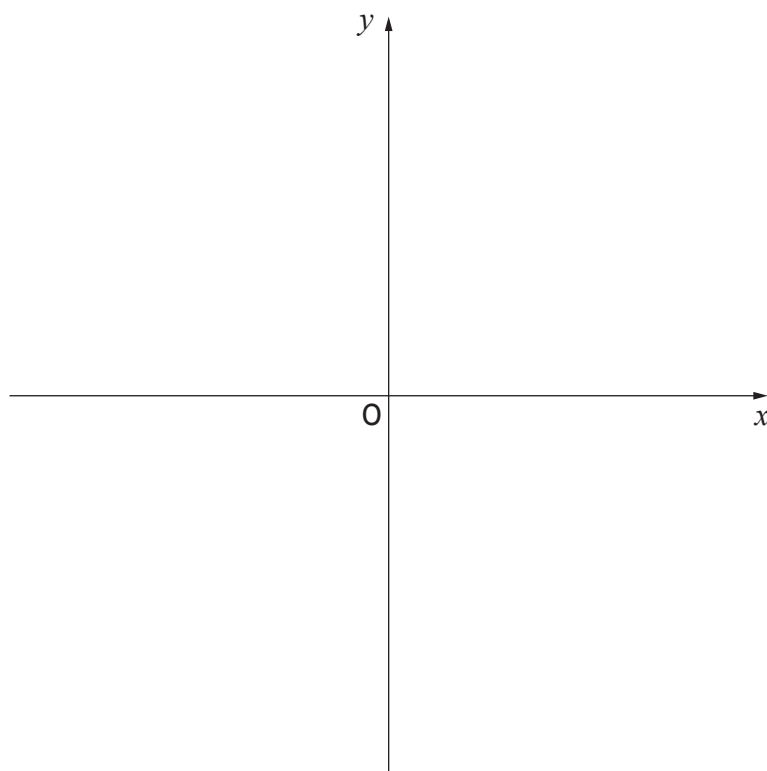
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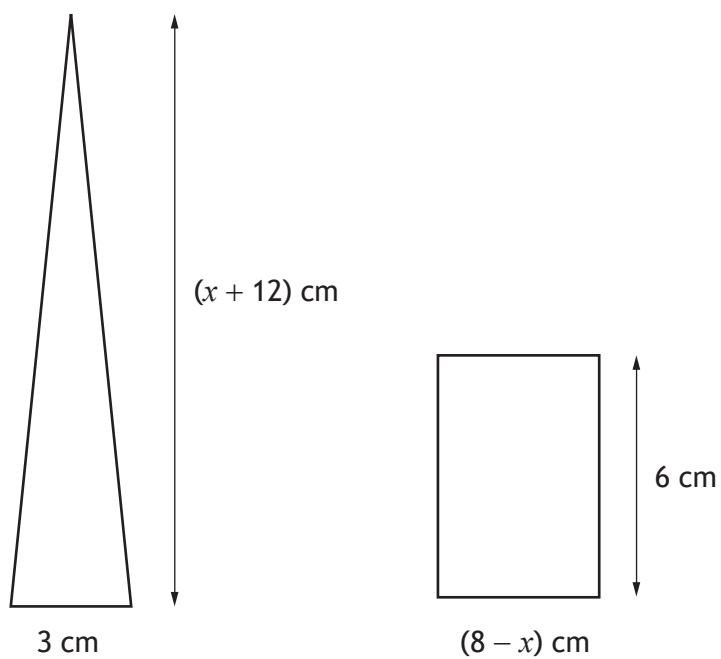
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14. Sketch the graph of  $y = (x + 1)(x - 3)$  using the axes provided below.  
 On your sketch, show clearly the points of intersection with the  $x$ -axis and the  $y$ -axis, and the coordinates of the turning point.  
 (Additional axes, if required, can be found on *page 14*.)

3



15. A triangle and rectangle are shown in the diagram.



(a) Find an expression for the area of the triangle.

1

15. (continued)

- (b) Given that the area of the triangle is equal to the area of the rectangle, find algebraically the value of  $x$ .

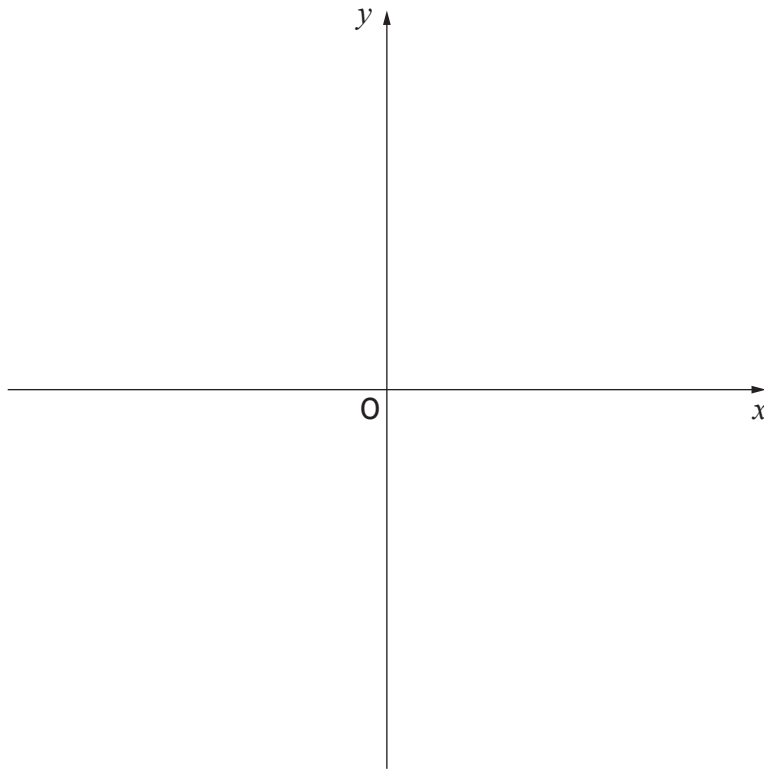
4

[END OF QUESTION PAPER]



ADDITIONAL SPACE FOR ANSWERS

Additional axes for question 14.



MARKS DO NOT  
WRITE IN  
THIS  
MARGIN

ADDITIONAL SPACE FOR ANSWERS



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\* X 8 4 7 7 5 0 1 1 6 \*