



# **GCSE MARKING SCHEME**

**MATHEMATICS - UNITISED**

**NOVEMBER 2014**

## **INTRODUCTION**

The marking schemes which follow were those used by WJEC for the November 2014 examination in GCSE MATHEMATICS - UNITISED. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.



GCSE Mathematics - Unitised Unit 1 Foundation Tier November 2014	Mark	Final Mark Scheme Comments																												
<p>5. (Rented out first year =) <math>\frac{3}{4} \times 60</math>  <math>= 45</math>  (Rent collected first year <math>45 \times (\pounds)150 =</math>) <math>(\pounds)6750</math>  (Rented out second year =) <math>0.8 \times 60</math>  <math>= 48</math>  (Rent collected second year = <math>48 \times 150 =</math>) <math>(\pounds)7200</math>    (Total collected over the two years =) <math>(\pounds)13950</math></p> <p>Look for</p> <ul style="list-style-type: none"> <li>• spelling</li> <li>• clarity of text explanations,</li> <li>• the use of notation (watch for the use of '=', '£' and '×' being appropriate)</li> </ul> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>AND</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul>	<p>M1 A1 A1 M1 A1 A1 B1</p> <p>QWC2</p> <p>9</p>	<p>F.T. their number of allotments.</p> <p>F.T. 'their 48' <math>\times \pounds 150</math>. Number of allotments rented must be different to number for first year.</p> <p>F.T. their two amounts.</p> <p><u>Alternative Methods</u></p> <p style="text-align: right;"><i>OR</i></p> <table style="width: 100%; border: none;"> <tr> <td style="padding: 2px;"><math>60 \times (\pounds)150</math></td> <td style="padding: 2px;"><i>M1</i></td> <td style="padding: 2px;"><math>\frac{3}{4} \times 60</math></td> <td style="padding: 2px;"><i>M1</i></td> </tr> <tr> <td style="padding: 2px;"><math>= (\pounds)9000</math></td> <td style="padding: 2px;"><i>A1</i></td> <td style="padding: 2px;"><math>= 45</math></td> <td style="padding: 2px;"><i>A1</i></td> </tr> <tr> <td style="padding: 2px;"><math>\frac{3}{4} \times (\pounds)9000</math></td> <td style="padding: 2px;"><i>M1</i></td> <td style="padding: 2px;"><math>0.8 \times 60</math></td> <td style="padding: 2px;"><i>M1</i></td> </tr> <tr> <td style="padding: 2px;"><math>= (\pounds)6750</math></td> <td style="padding: 2px;"><i>A1</i></td> <td style="padding: 2px;"><math>= 48</math></td> <td style="padding: 2px;"><i>A1</i></td> </tr> <tr> <td style="padding: 2px;"><math>0.8 \times (\pounds)9000</math></td> <td style="padding: 2px;"><i>M1</i></td> <td style="padding: 2px;"><math>(45+48 =) 93</math></td> <td style="padding: 2px;"><i>B1</i></td> </tr> <tr> <td style="padding: 2px;"><math>= (\pounds)7200</math></td> <td style="padding: 2px;"><i>A1</i></td> <td style="padding: 2px;"><math>93 \times (\pounds)150</math></td> <td style="padding: 2px;"><i>M1</i></td> </tr> <tr> <td style="padding: 2px;"><math>(Total =) (\pounds)13950</math></td> <td style="padding: 2px;"><i>B1</i></td> <td style="padding: 2px;"><math>(Total =) (\pounds)13950</math></td> <td style="padding: 2px;"><i>A1</i></td> </tr> </table> <p>QWC2. Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1. Presents relevant material in a coherent and logical manner, but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weakness in organisation of material but using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0. Evident weakness in organisation of material and errors in use of mathematical form, spelling, punctuation and grammar.</p>	$60 \times (\pounds)150$	<i>M1</i>	$\frac{3}{4} \times 60$	<i>M1</i>	$= (\pounds)9000$	<i>A1</i>	$= 45$	<i>A1</i>	$\frac{3}{4} \times (\pounds)9000$	<i>M1</i>	$0.8 \times 60$	<i>M1</i>	$= (\pounds)6750$	<i>A1</i>	$= 48$	<i>A1</i>	$0.8 \times (\pounds)9000$	<i>M1</i>	$(45+48 =) 93$	<i>B1</i>	$= (\pounds)7200$	<i>A1</i>	$93 \times (\pounds)150$	<i>M1</i>	$(Total =) (\pounds)13950$	<i>B1</i>	$(Total =) (\pounds)13950$	<i>A1</i>
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<p>6. Nigel 2 Rhian 6</p>	<p>B2</p> <p>2</p>	<p>Must be whole numbers. SC1 if reversed.</p> <p>B1 for 'their score for Rhian' = 'their score for Nigel' + 4.</p> <p>B1 for 'their score for Rhian' = 'their score for Nigel' <math>\times 3</math>.</p>																												
<p>7(a) (Insurance =) <math>(\pounds)144 - (\pounds)30 \times 4</math>  <math>= (\pounds)24</math></p> <p>(b) <math>(\frac{2}{3} \times \pounds 144 =)</math> <math>(\pounds)96</math>  (Each paid ) <math>\frac{(\pounds)144 - (\pounds)96}{2}</math>  <math>= (\pounds)24</math></p>	<p>M1 A1</p> <p>B1 M1</p> <p>A1</p> <p>5</p>	<p>Allow embedded answers.</p> <p>For sight of <math>(\pounds)96</math>. F.T. 'their <math>\pounds 96</math>'.</p> <p><u>Alternative Methods 7(b)</u></p> <table style="width: 100%; border: none;"> <tr> <td style="padding: 2px;"><math>(\frac{2}{3} \times \pounds 144 =)</math></td> <td style="padding: 2px;"><math>(\pounds)48</math></td> <td style="padding: 2px;"><i>OR</i></td> <td style="padding: 2px;"><i>Sight of</i> <math>\frac{1}{6}</math></td> <td style="padding: 2px;"><i>B1</i></td> </tr> <tr> <td style="padding: 2px;"></td> <td style="padding: 2px;"><math>(\pounds)48 \div 2</math></td> <td style="padding: 2px;"><i>OR</i></td> <td style="padding: 2px;"><math>\frac{1}{6} \times 144</math></td> <td style="padding: 2px;"><i>M1</i></td> </tr> <tr> <td style="padding: 2px;"></td> <td style="padding: 2px;"><math>= (\pounds)24</math></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"></td> <td style="padding: 2px;"><i>A1</i></td> </tr> </table>	$(\frac{2}{3} \times \pounds 144 =)$	$(\pounds)48$	<i>OR</i>	<i>Sight of</i> $\frac{1}{6}$	<i>B1</i>		$(\pounds)48 \div 2$	<i>OR</i>	$\frac{1}{6} \times 144$	<i>M1</i>		$= (\pounds)24$			<i>A1</i>													
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GCSE Mathematics - Unitised Unit 1 Foundation Tier November 2014	Mark	Final Mark Scheme Comments
8(a) Use of Volume = length $\times$ width $\times$ height. (Volume $\Rightarrow$ ) $3 \times 2 \times 0.5$ $= 3(\text{m}^3)$  (b) (Total length $\Rightarrow$ ) $3 + 2 + 3 + 2 + 4 \times 0.5$ $= 12(\text{m})$ (Cost $\Rightarrow$ ) $(\pounds)48$	M1 m1 A1  M1 A1 A1 6	Allow $3 \times 2 \times 50$ Also accept $300 \times 200 \times 50$ . C.A.O.  For attempt to add at least 5 lengths. C.A.O. F.T. $4 \times$ 'their total length'.
9(a) $480 \times 13.25$ $= 6360$ (rand)  (b) $795 \div 13.25$ $= (\pounds)60$ (A difference of) $(\pounds)8$	M1 A1  M1 A1 A1  5	F.T. 'their $(\pounds)60$ ' – $(\pounds)8$ . <u>Alternative method.</u> $795 - (52 \times 13.25)$ M1 (106 rand gains M1) $\div 13.25$ m1 $= (\pounds)8$ A1
10. $320 \times 1.6$ OR $480 \times 0.625$ $= 512$ (km) OR $= 300$ (miles)  (Difference $\Rightarrow$ ) 32km OR 20 miles AND 'England'	M1 A1  A1  3	Or equivalent e.g. $320 \times 8/5$ OR $480 \times 5/8$ .  F.T. their calculation if M1 awarded. Correct units must be given and England identified as the country in which most distance was covered.
11. (a) A comment that refers to the fact that the gradient of the 'Llankavani line' appears to be greater than that of the 'Rossmuch line'.  (b) Some reference made to the different scales used on either the vertical or the horizontal axis.  (c) Uniform vertical scale of $1\text{cm} \equiv 100$ complaints.  Line from (2004, 500) to (2014, 600) AND labelled 'Llankavani'. Line from (2004, 500) to (2014, 1000) AND labelled 'Rossmuch'.	E1  E1  B1  L1 L1  5	A reference to 'gradient (steeper)' gains E1. A reference to '(different) scale' gains E1. Allow these marks whether given in (a) or (b).  Allow $\pm 2\text{mm}$ . Allow 'notches' with no values written.  Allow intent for both L1 marks.  Penalise $-1$ if <u>both</u> lines start from (2004,0) or <u>both</u> lines start from (year,500) year $\neq$ 2004. Penalise $-1$ , once only, if lines continue significantly beyond 2014. B0, (possible)L1, L1 if no scale shown. SC1 if <u>both</u> lines 'correct' but not labelled or incorrectly labelled.



## UNIT 1 - HIGHER TIER

GCSE Mathematics - Unitised Unit 1 Higher Tier November 2014	Mark	Final Mark Scheme Comments
<p>1. (a) Question 2 because it is not relevant.</p> <p>(b) Two valid reasons given. E.g.                      “No box for ‘Never’”.                      “‘More than 10’ and ‘less than 20’ are not exclusive”.                      “Less than 20 overlaps all the other three answers”.                      “Over what period of time?”</p>	<p>B1</p> <p>B2</p> <p>3</p>	<p>Allow e.g. ‘not valid’ for ‘not relevant’.                      Do not credit ‘too personal’.                      Q2 with no reason, or an incorrect reason, is B0.</p> <p>B1 for each different reason (maximum of 2 marks).                      Ignore extra incorrect statements such as, ‘2<sup>nd</sup> and 3<sup>rd</sup> boxes overlap’ or ‘last box should be more than twenty’ if marks have been awarded for correct reasons.</p>
<p>2 (a) A comment that refers to the fact that the gradient of the ‘Llankavani line’ appears to be greater than that of the ‘Rossmuch line’.</p> <p>(b) Some reference made to the different scales used on either the vertical or the horizontal axis.</p> <p>(c) Uniform vertical scale of 1cm <math>\equiv</math> 100 complaints.</p> <p style="text-align: center;">Line from (2004, 500) to (2014, 600) AND labelled ‘Llankavani’.</p> <p style="text-align: center;">Line from (2004, 500) to (2014, 1000) AND labelled ‘Rossmuch’.</p>	<p>E1</p> <p>E1</p> <p>B1</p> <p>L1</p> <p>L1</p> <p>5</p>	<p>A reference to ‘gradient (steeper)’ gains E1. A reference to ‘(different) scale’ gains E1. Allow these marks whether given in (a) or (b).</p> <p>Allow <math>\pm 2</math>mm.                      Allow ‘notches’ with no values written.</p> <p>Allow intent for both L1 marks.</p> <p>Penalise –1 if <u>both</u> lines start from (2004,0) or <u>both</u> lines start from (year,500) year <math>\neq</math> 2004.</p> <p>Penalise –1, once only, if lines continue significantly beyond 2014.                      B0, (possible)L1, L1 if no scale shown.                      SC1 if <u>both</u> lines ‘correct’ but not labelled or incorrectly labelled.</p>
<p>3 (a) Samir AND a valid reason given.</p> <p>(b) Catrin AND a valid reason given.</p>	<p>B1</p> <p>B1</p> <p>2</p>	<p>e.g. ‘Most of his points were 3 or over’,                      ‘Samir had a mean of 3.5’.                      B0 if an incorrect mean given for Samir.</p> <p>e.g. ‘Samir’s range was (only) 3’ also allow ‘Samir’s range was 2 to 5 (or 5 to 2)’.                      B0 if an incorrect range given for Samir.</p>
<p>4. (Cost <math>\Rightarrow</math>) (£)27.50 <math>\times</math> 1.2 or equivalent.                      = (£)33                      (Change <math>\Rightarrow</math>) (£)7</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>3</p>	<p>FT 40 – ‘their 33’                      If no marks, SC1 for sight of (£)18.</p>



GCSE Mathematics - Unitised Unit 1 Higher Tier November 2014	Mark	Final Mark Scheme Comments	
7(a) Use of 'Distance' / 'Time' (Average speed =) $30 / 1.5$ $= 20$ (mph)  (b) Correct strategy.  Two different routes shown AND a correct distance given in each case.	M1 m1 A1  S1  B2  6	Allow 1(h)30(m) or 1.3 or 90(min) etc. for this M1.  C.A.O.  Shows understanding of table values with at least two distances correctly noted. B1 for each. A-B- D-C-A = 27(miles) A-C- B-D-A = 29(miles) A-C- D-B-A = 27(miles) A-D- B-C-A = 29(miles) A-D- C-B-A = 30(miles)	
8. Sight of either $\pi \times 5^2$ OR $\frac{1}{2} \times 8 \times 6$  (Area =) $\pi \times 5^2 - \frac{1}{2} \times 8 \times 6$ $= 54.5(\dots)$ $\text{m}^2$	B1  M1 A1 U1  4	$\pi \times 5^2$ must be for area of circle not semicircle. Allow B1 for $(\pi \times 5^2)/2$ if clearly area of semicircle. Look out for M0 for $\pi \times 5^2 - (6 + 8 + 10)$ . Accept 54.5 to 54.6 inclusive. Correct units for final answer. Independent of all other marks.	
9(a) $20^2 = 4^2 + 2 \times a \times 64$ $\frac{20^2 - 4^2}{2 \times 64}$ (= a) $= 3(\text{ms}^{-2})$  (b) $(v^2 =) 4^2 + 2 \times 3 \times 100$ (= 616) $(v =) 24.8(\dots)(\text{ms}^{-1})$ (so velocity of $25\text{ms}^{-1}$ not reached)	B1 B1  B1  M1 A1  5	For correct substitution.  F.T. their acceleration from part (a). A0 if 24.8 approximated to 25 and 'Yes' stated. <u>Alternative methods.</u> (Using $v = 25$ ) $a = \frac{25^2 - 4^2}{2 \times 100}$ OR $u^2 = 25^2 - 2 \times 3 \times 100$ M1 $= 3.045$ $u = 5$ So $a = 3$ not enough. So $u = 4$ not enough A1 ('not enough' must be indicated for A1) <u>Also (continuing from position reached in (a))</u> $(v^2 =) 20^2 + 2 \times 3 \times 36$ (= 616) M1 $(v =) 24.8(\dots)(\text{ms}^{-1})$ A1 (so velocity of $25\text{ms}^{-1}$ not reached)	
10. $125\% \equiv 297(\text{lb})$ (Initial weight =) $\frac{297 \times 100}{125}$ $= 237.6(\text{lb})$  $\approx \frac{237.6}{2.2}$ (kg) or $\frac{237.6 \times 5}{11}$ $= 108(\text{kg})$	B1 M1  A1  M1  A1  5	Accept any indication. Or equivalent e.g. $297 / 1.25$ .  F.T. 'their 237.6'.	<u>Alternative method</u> $\frac{297}{2.2}$ M1 $= 135(\text{kg})$ A1 $125\% \equiv 135$ B1 F.T. (Initial weight) $\frac{135 \times 100}{125}$ M1 $= 108(\text{kg})$ A1

GCSE Mathematics - Unitised Unit 1 Higher Tier November 2014	Mark	Final Mark Scheme Comments
11. $2 \times \frac{11}{8}$ or equivalent.  $\times \frac{40}{60}$ or equivalent $= 11/6$ (hrs)  $= 1\text{hrs } 50\text{min}$	M1  M1  A1  B1  4	M2 for correct use of the '2' with all four of the numbers 11, 8, 40 and 60. M1 for correct use of the '2' with any two of the numbers 11, 8, 40 and 60.  C.A.O. or equivalent e.g. 1.83...(hrs).  F.T. conversion from 'their 11/6' only if of equivalent difficulty (not 1/2 an hour). Allow 2hrs 11min or 2hrs 10min as FT from 2.18...hrs.
12. Sight of 19.5(min) AND 20.5(min) Sight of $24 \times 60 (= 1440)$ (min) $\frac{24 \times 60}{19.5}$ OR $\frac{24 \times 60}{20.5}$  73.8(...) AND 70.2(...)  (Greatest number =) 74 AND (Least number =) 71	B1 B1 M1  A1  A1  5	Accept 19min 30sec. AND 20min 30sec. for B1. May be implied in calculations. F.T numerator <u>only</u> for $24 \times 60 \times 60$ or $60 \times 60$ . F.T. if 'least $19 \leq t < 20$ OR greatest $20 < t \leq 21$ '.  F.T. 'their 73.8' AND 'their 70.2' rounded up. A0 for 73 and 70 (First capsule not considered).
13(a) $\frac{\theta \times \pi \times 20^2}{360} - \frac{\theta \times \pi \times 7^2}{360} = 199.1$ $(\theta =) \frac{199.1 \times 360}{\pi \times (20^2 - 7^2)} = 65(^{\circ})$  (b) Sight of $\frac{65}{360} \times 2 \times \pi \times 20$ OR $\frac{65}{360} \times 2 \times \pi \times 7$  $= 22.7$ OR $= 7.9$  (Perimeter =) $22.7 + 7.9 + 13 + 13 = 56.6$ (m)	M1  m1  A1  M1  A1  M1 A1 7	Or equivalent.  SC1 for 57(^{\circ})  FT 'their 65' for all 4 marks  Accept 22.6(...) and 7.9(...).  F.T. their 'arc lengths' only if the method used for finding each of the arcs is correct.
14 Sight of $\frac{2}{3} \times \pi \times 20^3$ or 16755(.1...) or $16000\pi/3$  Sight of $\frac{1}{3} \times \pi \times 15^2 \times h$  $\frac{1}{3} \times \pi \times 15^2 \times h = 9/40 \times \frac{2}{3} \times \pi \times 20^3$  (20 - d =) or (h =) $\frac{9 \times 2 \times \pi \times 20^3 \times 3}{40 \times 3 \times \pi \times 15^2}$ or equivalent. $= 16$ (cm)  (d =) 4(cm)	B1  B1  M1  A1  A1  A1 6	B0 if $\frac{2}{3} \times \pi \times 20^3$ evaluated incorrectly and <u>used</u> in further work. 'h' clearly being the height of the cone. May be written as (20 - d). Do not penalise lack of brackets at this stage.  F.T. 'their cone vol.' = $9/40 \times$ 'their hemisphere vol.' For M1. (l.h.s. = $235.6 \times h$ r.h.s. = 3769.9 or 3770). Allow M1 only if (20 - d) is used without acknowledgement of the brackets.  (3770 $\div$ 235.6)  F.T. 20 - 'their 16' if M1 gained.

**UNIT 2 - FOUNDATION TIER**

GCSE Mathematics - Unitised Unit 2 (non calculator) Foundation Tier November 2014	Mark	Final Mark Scheme Comments
<p>1. (a) (i) three hundred and forty six thousand, one hundred (ii) 42604 (b) 1122 (c) 32 (p) (d) 57 (e) 1, 3, 5, 15</p> <p>(f) 56 (g) <math>6 \times 20</math> (=) 120</p>	<p>B1 B1 B1 B1 B1 B2</p> <p>B1 M1 A1</p> <p>10</p>	<p>B1 for any 2 correct and no incorrect factors OR 3 correct and no more than 1 incorrect OR all 4 correct and 1 incorrect</p> <p>Accept <math>6 \times 21</math> or <math>6 \times 22</math> 126, 132 M0 A0 for <math>6 \times 21.8 = 130.8</math></p>
<p>2. (a) perpendicular</p> <p>(b) (i) straight line drawn joining 2 points on circumference passing through centre (ii) straight line touching circumference</p> <p>(c) </p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>4</p>	<p>Intention of one horizontal line of the correct length in the correct position</p>
<p>3.(a) 38 (b) - 15 (c) (i) <math>(x =) 33</math> (ii) <math>(x =) 100</math> (iii) <math>4x = 36</math> (<math>x =</math>) 9</p>	<p>B1 B1 B1 B1 B1 B1</p> <p>6</p>	<p>Accept embedded answers</p> <p>FT <math>x =</math> 'their <math>36/4</math>' Do not accept a final answer of <math>36/4</math>.</p>
<p>4.(a) likely (b) 10/127 (c) 6 triangles shaded</p>	<p>B1 B1 B1 3</p>	
<p>5. <math>(1000 \div 200)</math> 5 (packets) <math>5 \times (\pounds)3.50</math> (<math>\pounds</math>) 17.50</p>	<p>B1 M1 A1 3</p>	<p>FT 'their 5' if <math>1000 \div 200</math> or equivalent seen.</p>

<p align="center"><b>GCSE Mathematics - Unitised Unit 2 (non calculator) Foundation Tier November 2014</b></p>	<p align="center"><b>Mark</b></p>	<p align="center"><b>Final Mark Scheme Comments</b></p>
<p>6. 6:38 (pm. Put in oven.) 7:13 (pm. Remove from oven and stir. Replace in oven.) 7:28 (pm. Remove from oven.) (7:30 pm. Serve)</p> <p>QWC: Look for</p> <ul style="list-style-type: none"> <li>• relevance of work shown</li> <li>• generally correct spelling</li> <li>• clarity of text explanation</li> <li>• correct use of notation for time</li> </ul> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>e.g. show calculations with times given in the question</p> <p>AND</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their working</li> </ul> <p>(include p.m. and = when appropriate)</p> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in</li> </ul> <p>mathematical form, spelling, punctuation and grammar, and include units in their working.</p>	<p>B1 B1 B1</p> <p>QWC 2</p> <p>5</p>	<p>Do not penalise additional time added for removing from oven, stirring etc</p> <p><i>Alternative method:</i> <i>Times given with gaps of</i> 35 minutes    B1 15 minutes    B1 2 minutes AND finish at 7:30 pm B1</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar</p> <p>OR</p> <p>evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.</p> <p>Final unsupported statements only gets QWC0</p>



<p align="center"><b>GCSE Mathematics - Unitted Unit 2 (non calculator) Foundation Tier November 2014</b></p>	<p align="center"><b>Mark</b></p>	<p align="center"><b>Final Mark Scheme Comments</b></p>
<p>12. <u>Basic Membership</u> (Total cost for basic membership = ) <math>10 \times (\pounds)32 + (\pounds)4 \times 2 \times 52</math> or equivalent (Total cost for basic membership = ) <math>(\pounds)736</math></p> <p><u>Elite Membership</u> (Total cost for elite membership = ) <math>12 \times [(\pounds)60 - 0.1 \times (\pounds)60]</math> or equivalent (Total cost for elite membership = ) <math>(\pounds)648</math></p> <p>Conclusion that Elite Membership is cheaper AND by <math>(\pounds)88</math></p>	<p>M1 A1</p> <p>M1 A1</p> <p>B1</p> <p>5</p>	<p>A complete correct method Correct total for basic membership If no marks for ‘basic membership calculation’, award for SC1 for sight of <math>(12 \times (\pounds)32 + (\pounds)4 \times 2 \times 52 =) (\pounds)800</math> OR award SC1 for <math>(10 \times (\pounds)32 + (\pounds)4 \times 52 =) (\pounds)528</math></p> <p>A complete correct method Correct total for elite membership SC1 for sight of <math>(\pounds)54</math> or <math>(\pounds)72</math> if 2<sup>nd</sup> M0A0</p> <p>FT only if both M marks were awarded OR if first SC and second M marks were awarded.</p>
<p>13. <math>6 \times \frac{3}{4}</math> (= 18/4)</p> <p align="center"><math>4 \frac{1}{2}</math> (kg) (Requires <math>2 \times 2</math>(kg) tins and <math>1 \times \frac{1}{2}</math> (kg) tin) <math>(2 \times (\pounds)5.20 + 1 \times (\pounds)1.70)</math> <math>(\pounds)12.10</math></p>	<p>M1 A1</p> <p>A1</p> <p>3</p>	<p>Accept <math>\frac{3}{4} + \frac{3}{4} + \frac{3}{4} + \frac{3}{4} + \frac{3}{4} + \frac{3}{4}</math>.</p> <p>FT ‘their <math>4\frac{1}{2}</math>’ provided of equivalent difficulty If no marks, award SC1 for at least two correct costings of combinations (with at least 1 involving 2 or 3 sizes of tin and at least 1 involving a multiple).</p>
<p>14. (a) <math>7n - 2</math> (b) <math>20x^5</math></p>	<p>B2 B2</p> <p>4</p>	<p>B1 for <math>7n \pm \dots</math> or equivalent. B1 for <math>20x^m</math> or <math>nx^5</math> where <math>m</math> is an integer and <math>m \neq 0</math> or 1; <math>n</math> is an integer and <math>n \neq 0</math>.</p>
<p>15. (a) <math>108/360</math> or equivalent (e.g. <math>3/10</math>)</p> <p>(b) Sight of <math>1 - 3/10</math> (= <math>7/10</math>) or equivalent</p> <p align="center"><math>7/10 \times 720</math> 504</p>	<p>B2</p> <p>M1 m1 A1</p> <p>5</p>	<p>B1 for numerator of 108 or denominator of 360 in a fraction <math>&lt; 1</math> Mark final answer.</p> <p>FT ‘their <math>3/10</math>’ (but not for an answer of <math>1/2</math>).</p> <p>If 0 marks, SC1 for sight of 216.</p> <p><i>Alternative method:</i> <math>3/10 \times 720 (=216)</math> M1 FT ‘their <math>3/10</math>’ <math>720 - 216</math> m1 504 A1</p>

## UNIT 2 - HIGHER TIER

GCSE Mathematics - Unitised Unit 2 Higher Tier November 2014	Mark	Final Mark Scheme Comments
(b) 1. Correct reflection	B2  2	B1 for a reflection in any horizontal line or in $x = 3$ or sight of the line $y = 3$
<p>2. <u>Basic Membership</u> (Total cost for basic membership = ) <math>10 \times (\pounds)32 + (\pounds)4 \times 2 \times 52</math> or equivalent (Total cost for basic membership = ) <math>(\pounds)736</math></p> <p><u>Elite Membership</u> (Total cost for elite membership = ) <math>12 \times [(\pounds)60 - 0.1 \times (\pounds)60]</math> or equivalent (Total cost for elite membership = ) <math>(\pounds)648</math></p> <p>Conclusion that Elite Membership is cheaper AND by <math>(\pounds)88</math></p> <p>Look for</p> <ul style="list-style-type: none"> <li>• relevance</li> <li>• spelling in at least 1 statement/sentence</li> <li>• clarity of text explanations,</li> <li>• the use of notation (watch for the use of '=', £, % being appropriate)</li> </ul> <p>A clear conclusion statement must be made before QWC2 can be awarded.</p> <p>Count incorrect use of '=' in situations such as '<math>4 \times 2 \times 52 = 416 + 320</math>' within the 'few errors in mathematical form'</p> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>AND</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units (£) in their final answer</li> </ul> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units (£) in their final answer</li> </ul>	<p>M1 A1</p> <p>M1 A1</p> <p>B1</p> <p>Q W C 2</p> <p>7</p>	<p>A complete correct method. Correct total for basic membership. If no marks for 'basic membership calculation', award for SC1 for sight of <math>(12 \times (\pounds)32 + (\pounds)4 \times 2 \times 52 =) (\pounds)800</math> OR award SC1 for <math>(10 \times (\pounds)32 + (\pounds)4 \times 52 =) (\pounds)528</math></p> <p>A complete correct method. Correct total for elite membership. SC1 for sight of <math>(\pounds)54</math> or <math>(\pounds)72</math> if 2<sup>nd</sup> M0A0.</p> <p>FT only if both M marks were awarded OR if first SC and second M marks were awarded.</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.</p> <p>A final unsupported statement only gets QWC0.</p>
(c) 3. $(a = ) 63$ (°) $(b = ) 117$ (°)	B1 B1 2	FT 180 - 'their $a$ '.



GCSE Mathematics - Unitised Unit 2 Higher Tier November 2014	Mark	Final Mark Scheme Comments
11. (a) $10x^2 + 5xy - 4xy - 2y^2$ $10x^2 + xy - 2y^2$ or equivalent  (b) $2(2x - 1) + 3 = x - 5$  $3x = -6$  $x = -2$	B1 B1  M2  A1  A1 6	FT from 3 correct terms.  M1 for correctly cleared fractions by a valid method for any 2 terms. Collecting terms. FT provided at least M1 awarded.
12. Angle BAD = $180^\circ - 2x^\circ$ (angles in an isosceles triangle)  Angle BCD = $180^\circ - \text{Angle BAD}$ OR $180^\circ - [180^\circ - 2x^\circ]$ $(y) = 2x^\circ$ (opposite angles in a cyclic quadrilateral add up to $180^\circ$ )	B1  B1  B1  3	Check diagram. Allow first B1 without a full reason.  Second B1 is for clear use of cyclic quadrilateral.  Indication of correct circle theorem in words.
13. (a) 6  (b) $(\sqrt{16 \times 2} - \sqrt{2})^2$ or $32 - \sqrt{32}\sqrt{2} - \sqrt{32}\sqrt{2} + 2$ $(3\sqrt{2})^2$ or middle term = $\pm 8 \pm 8$ 18 <b>and</b> rational	B3  M1 M1 A1 6	B2 for $((1/25)^{-3} =) 5$ OR B2 for $1 + (1/5)^{-1}$ or $1 + 25^{\frac{1}{2}}$ or $1 + \sqrt{25}$ or $1 + 1/0.2$ B1 for $(4^0 =) 1$ OR for $(1/5)^{-1}$ or $25^{\frac{1}{2}}$ or $\sqrt{25}$  RHS method needs 3 of 4 terms correct; accept $\sqrt{64}$ as $\sqrt{32}\sqrt{2}$
14. (a) sight of $5/12 \times 1/11$ OR $1/12 \times 5/11$ $5/12 \times 1/11 + 1/12 \times 5/11$ OR $5/12 \times 1/11 \times 2$ $= 10/132 (= 5/66)$  (b) $1 - P(\text{no red ball})$ OR other <u>complete</u> method  $= 1 - 7/12 \times 6/11$ $(= 1 - 42/132)$ $= 90/132 (= 15/22)$	M1 M1 A1  S1  M1  A1 6	Complete correct method. ISW  $P(RR) + P(RR') + P(R'R)$ or $P(RR) + P(RW) + P(WR) + P(RG) + P(GR)$ or correct numerical equivalent.  Calculations showing correct sum of products of probabilities (without replacement). ISW
15. Reflection in y axis Curve passes through (0, 4) AND (-3, 0)	B1 B1 2	Clear intention shown. Co-ordinates need not be stated.

### UNIT 3 - FOUNDATION TIER

GCSE Mathematics - Unitised Unit 3 (calculator allowed) Foundation Tier November 2014	Mark	Final Mark Scheme Comments
1. (a) (£)8·5(0)  (£)23·85 (£)9·98 (£)42·33 (b) (£)7·67 (c) 6×1·99 (£)11·94	B1 B1 B1 B1 B1 B1 B1 7	FT candidate's values, provided equivalent difficulty FT 50 – 'their 42·33'. Or equivalent SC1 for $(9 \times 1 \cdot 99) = (£)17 \cdot 91$
2. (a) 53000  (b) 67 (c) 37·8	B1 B1 B1 3	
3. 42 – (38 – 12)  16	M1 A1 2	Or equivalent
4. $(6435 - 5793) = 642$ (units used)  $642 \times 15(p)$ (£)96·3(0) or 9630(p)	B1 M1 A1 3	FT 'their 642' from working If given, £ and/or p must be correct
5 Evidence of counting squares 48-52 (squares) 240-260 (m <sup>2</sup> )	M1 A1 B1 3	F.T. 5× 'their number of squares'
6. (a) A and L OR F and J (b) H and C	B1 B1 2	
7. (a) (i) any correct combination using 5, 3, 12 and 20.  (ii) any correct combination  (b) (i) 11 (ii) $4 \times 9 \div (3 - 1)$  (c) $-10 + -5$ (d) $-4 \times -6$	B1  B1  B1 B1  B1 B1 6	$5 + 3 = 20 - 12$ $12 + 5 = 20 - 3$ $12 + 3 = 20 - 5$ Accept answers in boxes or on lines $20 \div 5 = 12 \div 3$ or $5 \div 3 = 20 \div 12$ (incl reciprocals) Accept answers in boxes or on lines  A pair of brackets inserted correctly around subtraction. Extra brackets accepted if correct. Eg. $(4 \times 9) \div (3 - 1)$  Select the two negative numbers. In any order

GCSE Mathematics - Unitised Unit 3 (calculator allowed) Foundation Tier November 2014	Mark	Final Mark Scheme Comments
<p>8. Choosing a combination of 4 and 6 to make 16. 4, 4, 4, 4 or 6, 6, 4 Correct costing for one combination (£) 12 or (£) 11.6(0) (£) 11.6(0) and a convincing argument that 6, 6, 4 is cheapest OR both costings evaluated with a final answer of (£) 11.6(0)</p> <p>Look for</p> <ul style="list-style-type: none"> <li>• Spelling</li> <li>• Clarity of text explanations,</li> <li>• Consistent and correct use of £ or p signs.</li> </ul> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• Present work clearly, with words explaining process and steps</li> </ul> <p>AND</p> <ul style="list-style-type: none"> <li>• Make few, if any, mistakes in mathematical form, spelling, punctuation and grammar in their final answer.</li> </ul> <p>QWC1 : Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• Present work clearly, with words explaining process or steps</li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li>• Make few, if any, mistakes in mathematical form, spelling, punctuation and grammar in their final answer.</li> </ul>	<p>B1 B1 B1</p> <p>QWC 2</p> <p>5</p>	<p><b>Alternative method</b> Cost of 1 bottle from 6-bottle pack = <math>(£)4 \cdot 30 \div 6 =</math> <math>(£)0 \cdot 71(6)</math>. Cost of 1 bottle from 4-bottle pack = <math>(£)0 \cdot 75</math>. B1 for both. B1 for “Buy 2 6-bottle packs + 1 4 6-bottle pack”. B1 for correct total price <math>(£) 11 \cdot 6(0)</math></p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weakness in organisation of material but using acceptable mathematical form, with few, if any, errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weakness in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar.</p>
<p>9. A: 12 (‘sides’) <math>(36 \div 12 =) 3(\text{cm})</math></p> <p>(Perimeter B= <math>10 \times 3</math>) 30 (cm)</p>	<p>B1 B1 B1 3</p>	<p>Attempt to find the side length of a square. FT candidate’s number of ‘sides’ on perimeter A. No FT for <math>36 \div 5</math> FT <math>10 \times</math> times ‘their 3’ If no marks awarded, SC1 for B has perimeter of 10 ‘sides’.</p>
<p>10. (a) 18 (b) <math>120 = 45 + 5Y</math> <math>5Y = 75</math> <math>Y = 15</math></p>	<p>B1 B1 B1 B1 4</p>	<p>Correct substitution Isolating the Y. Accept <math>5Y = 120 - 45</math> F.T if <math>aY = b</math> (<math>a \neq 1</math>)</p>

GCSE Mathematics - Unitted Unit 3 (calculator allowed) Foundation Tier November 2014	Mark	Final Mark Scheme Comments
11.(a) 39  (b) D 5, C 9, B 6, A 4  (c) 21 to 30 or C (d) <b>Use overlay</b> 3 or 4 angles correct and correctly labelled  3 or 4 angles correct, labels not fully correct 2 angles correct and correctly labelled. 2 angles correct, labels not fully correct. 1 angle correct and correctly labelled.  OR <u>If 0 or 1 for the diagram or no diagram</u> 360/24 Angles are 75, 135, 90, and 60.	B1  B2  B1  B4  OR  B3 B3 B2 B1  OR  M1 A1 8	B1 for any two/three correct frequencies If frequencies score zero then B1 for all correct tallies. FT from their frequencies  Ft from their frequencies  If only B1 is scored for the diagram, and all the angles given correctly, then cancel the B1 and award M1, A1. If B0 scored for the diagram, check the angles and the method to see if the M1 and the A1 can be awarded.  (1 is) 15° gets M1. Or SC1 for all correct percentages. 20·8, 37·5, 25, 16·7
12. 3 (or 4) arcs and the bisector of the angle drawn.	B2  2	B1 for the first arc crossing both lines (or two equal radius arcs crossing both lines) <b>and</b> an attempt at the next stage in the construction.
13. (a) $45 \times 32 \times 30$ 43200 $\text{cm}^3$ (b) use of 1 litre = 1000 $\text{cm}^3$ (eg 43L = 43000 $\text{cm}^3$ ) (43litres is less than the volume of the tank) The water will not overflow	M1 A1 U1 M1  A1  5	Or equivalent  Accept ml  May be implied but not stated explicitly. Eg. 200 $\text{cm}^3$ space left. FT candidate's volume of tank provided M1 awarded in part (a).
14. $2/8$ is 48(pupils) or $1/4$ is 48(pupils) $48 \times 4$ or equivalent 192	B1 M1 A1 3	
15. $180 - (360/5)$ OR $((5-2) \times 180) / 5$ 108 (°)	M1 A1 2	Or equivalent
16. Area of one rectangle correctly evaluated (e.g. whole mirror) Area of two or more different white or black rectangles correctly evaluated A complete method of subtracting or adding areas e.g. 800 – (2×20×2 + 2×40×2 – 4×2×2) mirror      wooden strips      overlap = 576( $\text{cm}^2$ )	B1  B1  M1  A1 4	Possible calculation for the white pieces: 4 corner pieces $4 \times 2 \times 2$ (assuming squares) 2 long rectangles $2 \times 12 \times 2$ 2 tall rectangles $2 \times 32 \times 2$ Centre piece $12 \times 32$ Or BIBIMIAI for $36 \times 16 = 576(\text{cm}^2)$  CAO
17 (a) All points plotted correctly.  (b) Appropriate straight line of best fit drawn with some values above and below the line.  (c) from their line of best fit $\pm 0.05$ (tonnes).	B2  B1  B1 4	B1 for 3, 4 or 5 points plotted correctly, not joined, or B1 for all points plotted correctly but joined. Mark intention.  FT from their line. B0 if no line drawn.

GCSE Mathematics - Unitised Unit 3 (calculator allowed) Foundation Tier November 2014	Mark	Final Mark Scheme Comments																																																
18. Line or curve drawn from end of existing line to (08:30,0). Straight line drawn from (08:30,0) to (08:45, 15:00).	B1  B2  3	FT their first line. B1 for straight line drawn from (08:30,0) with correct gradient (500m every 5min) but not finishing at (08:45 , 15: 00) , OR B1 for straight line finishing at the school with correct gradient but not starting immediately after the first line.																																																
19. One correct evaluation $1.5 \leq x \leq 1.6$  2 correct evaluations $1.585 \leq x \leq 1.6$ one either side of 0  2 correct evaluations $1.585 \leq x \leq 1.595$ one either side of 0  <i>If evaluations not seen, accept 'too high' or 'too low'.</i> $x = 1.59$	B1  B1  M1    A1    4	<table border="0"> <tr> <td><math>x</math></td> <td><math>x^3 + 10x - 20</math></td> <td><math>x</math></td> <td><math>x^3 + 10x - 20</math></td> </tr> <tr> <td>1.5</td> <td>-1.625</td> <td>1.591</td> <td>-0.063</td> </tr> <tr> <td>1.51</td> <td>-1.457</td> <td>1.592</td> <td>-0.045</td> </tr> <tr> <td>1.52</td> <td>-1.288</td> <td>1.593</td> <td>-0.028</td> </tr> <tr> <td>1.53</td> <td>-1.118</td> <td>1.594</td> <td>-0.010</td> </tr> <tr> <td>1.54</td> <td>-0.948</td> <td>1.595</td> <td>0.008</td> </tr> <tr> <td>1.55</td> <td>-0.776</td> <td>1.596</td> <td>0.025</td> </tr> <tr> <td>1.56</td> <td>-0.604</td> <td>1.597</td> <td>0.043</td> </tr> <tr> <td>1.57</td> <td>-0.430</td> <td>1.598</td> <td>0.061</td> </tr> <tr> <td>1.58</td> <td>-0.256</td> <td>1.599</td> <td>0.078</td> </tr> <tr> <td>1.59</td> <td>-0.080</td> <td></td> <td></td> </tr> <tr> <td>1.6</td> <td>0.096</td> <td></td> <td></td> </tr> </table> <p>The second B1 can be gained by calculating one value that is too low in the range 1.585 to 1.6 AND stating clearly that 1.6 will be too high.</p>	$x$	$x^3 + 10x - 20$	$x$	$x^3 + 10x - 20$	1.5	-1.625	1.591	-0.063	1.51	-1.457	1.592	-0.045	1.52	-1.288	1.593	-0.028	1.53	-1.118	1.594	-0.010	1.54	-0.948	1.595	0.008	1.55	-0.776	1.596	0.025	1.56	-0.604	1.597	0.043	1.57	-0.430	1.598	0.061	1.58	-0.256	1.599	0.078	1.59	-0.080			1.6	0.096		
$x$	$x^3 + 10x - 20$	$x$	$x^3 + 10x - 20$																																															
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20. (Distance <sup>2</sup> =) $4 \cdot 9^2 - 4^2$ Distance <sup>2</sup> = 8.01 OR (Distance =) $\sqrt{8.01}$ (Distance =) 2.8(30...) (m)	M1 A1 A1 3																																																	
21. Sight of the mid-points 77.5, 82.5, 87.5, 92.5 $77.5 \times 4 + 82.5 \times 13 + 87.5 \times 17 + 92.5 \times 6$ (=3425 ) (310 + 1072.5 + 1487.5 + 555) $\div 40$ = 85(.625) (yards)	B1 M1  m1 A1 4	FT their mid-points from within or at the bounds of the groups																																																

### UNIT 3 - HIGHER TIER

GCSE Mathematics - Unitted Unit 3 Higher Tier November 2014	Mark	Final Mark Scheme
1. $-20 + 9.8 \times 5$ $= 29$	M1 A1 2	
2. All three amounts correct in comparable form e.g. 20%, 30%, 50%, OR 0.2, 0.3, 0.5 or equivalent  2:3:5	B2  B1 3	Allow fractions of a sum of money. B1 for any 2 amounts correct in comparable form.
3. (a) All points plotted correctly.  (b) Appropriate straight line of best fit drawn with some values above and below the line.  (c) from their line of best fit $\pm 0.05$ (tonnes).	B2  B1  B1 4	B1 for 3, 4 or 5 points plotted correctly, not joined, or B1 for all points plotted correctly but joined. Mark intention.  FT from their line. B0 if no line drawn.
4. (a) Line or curve drawn from end of existing line to (08:30,0). Straight line drawn from (08:30, 0) to (08:45, 15:00).  (b) $08:45 - 08:30$ $= 15$ (min)	B1  B2  M1 A1 5	FT their first line. B1 for straight line drawn from (08:30,0) with correct gradient. (500m every 5min) but not finishing at (08:45, 15:00), OR B1 for straight line finishing at the school with correct gradient but not starting immediately after the first line. FT 'their 08:45'.
5. $180 - (360/5)$ OR $((5-2) \times 180) / 5$ 108 ( $^{\circ}$ )	M1 A1 2	Or equivalent.
6. Suitable arcs drawn for $60^{\circ}$ angle. $60^{\circ}$ angle drawn with line 6cm long. Correct arcs drawn from the ends of the 10cm and 6cm lines. Lines of length 7cm and 4cm joining to complete the quadrilateral.	M1 A1 B1  B1 4	Allow $\pm 2^{\circ}$ for the $60^{\circ}$ angle, $\pm 2$ mm for all lengths.  Only award this B1 for the quadrilateral shown.
7. Area of one rectangle correctly evaluated (e.g. whole mirror) Area of two or more different white or black rectangles correctly evaluated  A complete method of subtracting or adding areas e.g. $800 - (2 \times 20 \times 2 + 2 \times 40 \times 2 - 4 \times 2 \times 2)$ mirror wooden strips overlap $= 576(\text{cm}^2)$  QWC: Look for <ul style="list-style-type: none"> <li>• correct units used i.e. <math>\text{cm}^2</math></li> <li>• correct use of mathematical notation e.g. +, -, =.</li> <li>• spelling in at least 1 statement/sentence</li> <li>• clarity of text explanations</li> </ul> QWC2: Candidates will be expected to <ul style="list-style-type: none"> <li>• present work clearly, with words or quantities shown for clarity of process or steps</li> </ul> AND <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar in their answer</li> </ul> QWC1: Candidates will be expected to <ul style="list-style-type: none"> <li>• present work clearly, with words or quantities shown for clarity of process or steps</li> </ul> OR <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar in their answer</li> </ul>	M1 B1  M1  A1  QWC 2  6	<p style="text-align: center;"><i>Possible calculation for the white pieces:</i>  <i>4 corner pieces <math>4 \times 2 \times 2</math> (assuming squares)</i>  <i>2 long rectangles <math>2 \times 12 \times 2</math></i>  <i>2 tall rectangles <math>2 \times 32 \times 2</math></i>  <i>Centre piece <math>12 \times 32</math></i>  <i>OR B1B1M1A1 for <math>36 \times 16 = 576(\text{cm}^2)</math></i></p> <p>CAO</p> <p>QWC2 Presents material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar</p> <p>OR</p> <p>evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.</p>

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8. (a) 2.4 or $2\frac{2}{5}$ (b) $8x - 20 = 3x - 5$ $5x = 15$ $x = 3$  (c) One correct evaluation $1.5 \leq x \leq 1.6$  2 correct evaluations $1.585 \leq x \leq 1.6$ one either side of 0  2 correct evaluations $1.585 \leq x \leq 1.595$ one either side of 0  <i>If evaluations not seen, accept 'too high' or 'too low'.</i> $x = 1.59$	B1 B1 B1 B1  B1  B1  M1  A1  8	FT until 2 <sup>nd</sup> error.  $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.5 & -1.625 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.591 & -0.063 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.51 & -1.457 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.592 & -0.045 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.52 & -1.288 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.593 & -0.028 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.53 & -1.118 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.594 & -0.010 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.54 & -0.948 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.595 & 0.008 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.55 & -0.776 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.596 & 0.025 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.56 & -0.604 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.597 & 0.043 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.57 & -0.430 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.598 & 0.061 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.58 & -0.256 \end{array} \quad \begin{array}{cc} x & x^3 + 10x - 20 \\ 1.599 & 0.078 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.59 & -0.080 \end{array}$ $\begin{array}{cc} x & x^3 + 10x - 20 \\ 1.6 & 0.096 \end{array}$ The 2 <sup>nd</sup> B1 can be gained by calculating a value that is too low in the range 1.585 to 1.6 AND stating clearly that 1.6 will be too high.
9. (First 2000 units cost) 13766(p) OR (£)137.66 (Remaining 16000 units cost) 47792(p) OR (£)477.92  $1.05 \times 61558$ OR $1.05 \times 615.58$ (Total cost including VAT =) 64635.9(p) OR (£) 646.359 Monthly payment = £ 53.86	B1 B1  M1 A1 A1 5	FT provided at least B1 awarded and both amounts considered. Accept rounded or truncated answer, to nearest penny. Must be correct to nearest penny.
10. (Distance <sup>2</sup> =) $4.9^2 - 4^2$ Distance <sup>2</sup> = 8.01 OR (Distance =) $\sqrt{8.01}$ (Distance =) 2.8(30...) (m)	M1 A1 A1 3	
11. Sight of the mid-points 77.5, 82.5, 87.5, 92.5 $77.5 \times 4 + 82.5 \times 13 + 87.5 \times 17 + 92.5 \times 6$ (=3425) $(310 + 1072.5 + 1487.5 + 555)$ $\div 40$ $= 85(.625)$ (yards)	B1 M1  m1 A1 4	FT their mid-points from within or at the bounds of the groups.
12. $12/\tan 72^\circ$ $= 3.8(990\dots)$ $AC = 7.79(80\dots)$ OR 7.8	M2 A1 A1 4	M1 for $\tan 72^\circ = 12/x$  Only accept 8 from correct working
13. Correct numerical representation of the numbers involved e.g. 500,000,000,000 or $5 \times 10^{11}$ or $500 \times 10^9$ Multiplication using the correct numbers $= 1.5 \times 10^{23}$	B1  M1 A1  3	Accept correct representation of one of the numbers.  If no marks gained, SC1 for an answer expressed in standard form following through from their consistent representation of each number.
14. OA=OC (or OA=OD) and OB=OD (or OB=OC) (all radii) AND angle AOB = angle COD (vertically opposite angles)  (Therefore the triangles are congruent) SAS	M2  A1 3	M1 for one correct statement. These may be seen on the diagram.  <i>One alternative method: M2 angle BAO = angle DCO and angle ABO = angle CDO (angles in the same segment) AND AO = OC (both radii). M1 for 1 pair of equal angles and equal radii. A1 for triangles are congruent (AAS).</i>
15. (a) $3a^2(3ab + 2)$  (b) $(x + 10)(x - 2)$ $x = -10$ AND $x = 2$	B2  M2 A1 5	B1 for $3a^2(3ab + \dots)$ OR $3a^2(\dots + 2)$ OR for correct partial factorisation. M1 for $(x \dots 10)(x \dots 2)$ FT their brackets, providing M1 awarded
16. (Volume of cube =) $343 \text{ (cm}^3\text{)}$ (Volume of a sphere =) $\frac{4}{3} \times \pi \times 1.5^3$ $= 14.13$ to $14.14 \text{ (cm}^3\text{)}$ (Maximum number of spheres =) $343/14.1\dots$ $= 24$	B1 M1 A1 M1 A1 5	Accept sight of 343 in working.  FT their values provided first M1 awarded. FT provided rounding required.

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17. (PQ =) $(12.6/\sin 44) \times \sin 28$ (PQ =) 8.5(154...) (cm)	M2 A1 3	M1 for $PQ/\sin 28 = 12.6/\sin 44$ or equivalent
18. Volume scale factor = $3510/130$ = 27 Length scale factor = 3 Height of water = $12/3 = 4$ (cm)	M1 A1 M1 A1  4	FT cube root of their 27 provided M1 awarded.  <i>Alternative:</i> M2 for $h^3 = 12^3 \times 130/3510$ . M1 for $(h/12)^3 = 130/3510$ or equivalent. m1 for $h = \sqrt[3]{12^3 \times \frac{130}{3510}}$ . A1 for 4(cm).
19. (a) $5(x+1) + 4(x-2)$ as numerator AND $(x-2)(x+1)$ as denominator OR multiply throughout by $(x-2)$ and $(x+1)$ $5(x+1) + 4(x-2) = 2(x-2)(x+1)$ $0 = 2x^2 - 11x - 1$ (b) $x = \frac{11 \pm \sqrt{(-11)^2 - 4 \times 2 \times (-1)}}{2 \times 2}$  $x = \frac{11 \pm \sqrt{129}}{4}$  $x = 5.59$ and $x = -0.09$ (Answers to 2 d.p.)	M2  A1 A1 M1  A1 7	Brackets required or implied later. M1 for either correct numerator or denominator, or multiply throughout with 1 error.  convincing Allow one error, in sign or substitution, but not in the formula  CAO  CAO
20. (a) Uniform scale on the vertical axis starting at 0 in blocks of 0.5. Appropriate width bars of height 1.4, 2.6, 2.  (b) 6	B1  B2  B1 4	FT their scale for all remaining marks provided not frequencies used. B1 for 2 correct bars or B1 for sight of correct frequency densities stated.
21. a) Tangent drawn at $x = 1$ . Idea of increase in $y$ /increase in $x$ . Gradient from a reasonable tangent. (b) Split into 3 areas and attempt to sum (Area =) $\frac{1}{2} \times 1(3 + 2 \times 5 + 2 \times 11 + 21)$ = 28 (units <sup>2</sup> )	S1 M1 A1 A1 M1 M1 A1 6	<i>Alternative method: M1 for <math>(dy/dx) = 4x</math> A1 for <math>4 \times 1</math> A1 for 4</i>  Or equivalent. Award for up to 1 error in reading scale. CAO



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